

Signatures of degree-3 tidal loading effects in superconducting gravimeter records predicted by data-unconstrained ocean tide modeling

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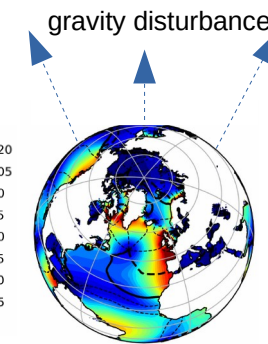
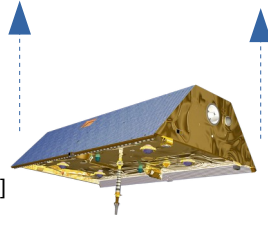
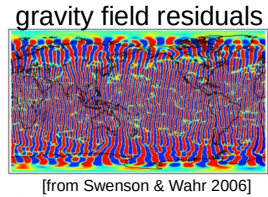
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Ocean tide modeling for satellite gravimetry

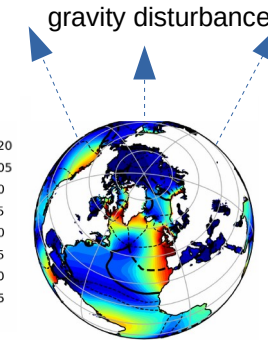
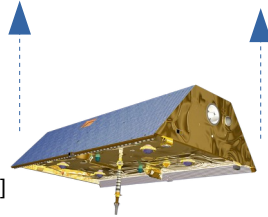
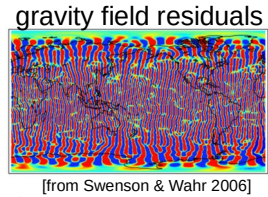
- Dealiasing of GRACE(-FO) data by application of background models
→ Imperfections induce significant residuals into gravity solutions (Flechtner, 2016)



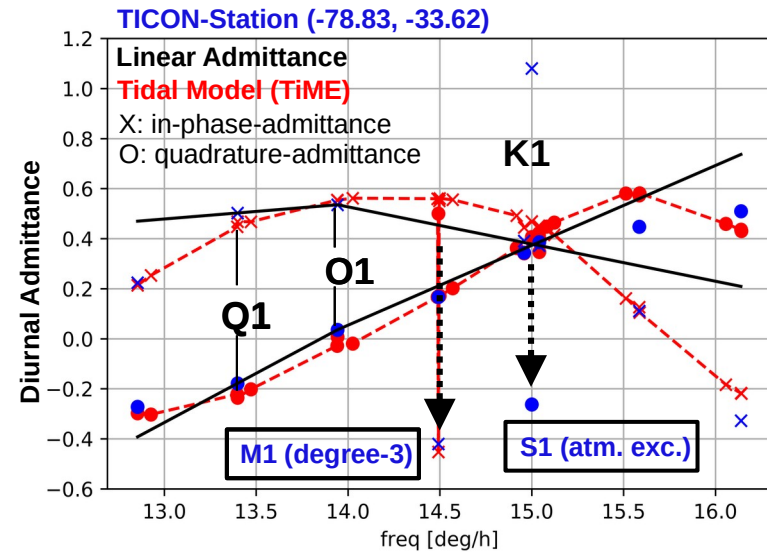
Periodic tidal mass redistribution

Ocean tide modeling for satellite gravimetry

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- Ocean tidal dynamics can be decomposed into a set of partial tides
→ Small amplitude tides are usually derived with admittance assumptions

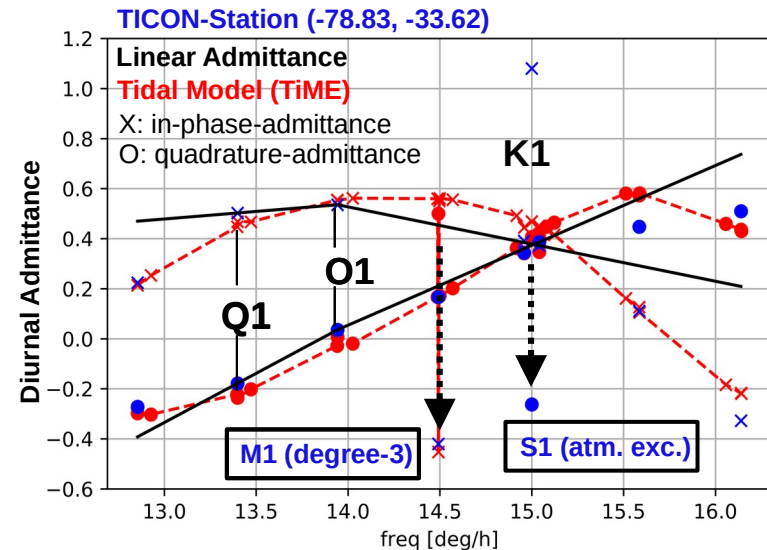
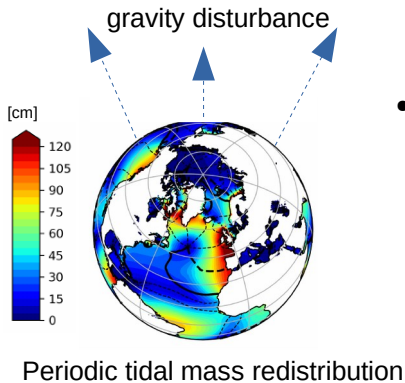
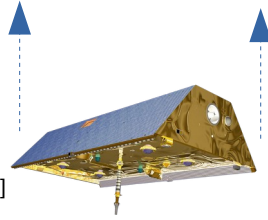
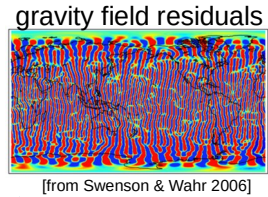


Periodic tidal mass redistribution



Ocean tide modeling for satellite gravimetry

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- Ocean tidal dynamics can be decomposed into a set of partial tides
→ Small amplitude tides are usually derived with admittance assumptions
- Admittance assumptions break down for atmospherically excited ocean tides (e.g. S1), and **degree-3 ocean tides**
→ Individual partial tide solutions required



Barotropic Ocean Tide Modeling and Validation

MODELING

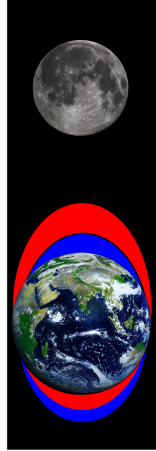
VALIDATION

Barotropic Ocean Tide Modeling and Validation

MODELING

Tide-Raising Forces

The lunar tide-raising potential possesses an **asymmetric part** described in first order by degree-3 spherical harmonic functions



VALIDATION

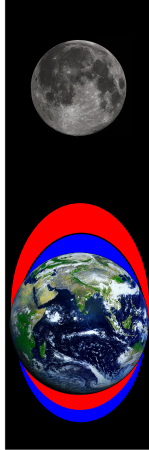
Barotropic Ocean Tide Modeling and Validation

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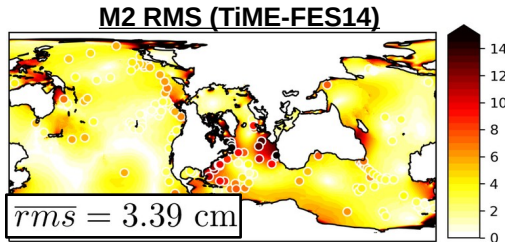
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Ocean Tide Model

We employ the ocean tide model TiME (Sulzbach, 2021)



Model characteristics:

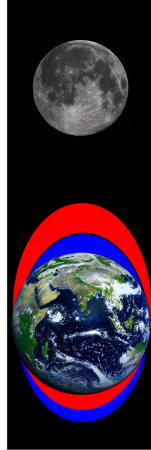
- data-unconstrained, finite-differences
- 1/12 ° resolution, **rotated poles**
- energy dissipation: bottom friction, param. eddy-viscosity and **wavedrag**
- Consideration of the non-local effect of Self-attraction and Loading (**SAL**)
- **rtopo2 bathymetry** including cavities below the Antarctic ice-shelf

Barotropic Ocean Tide Modeling and Validation

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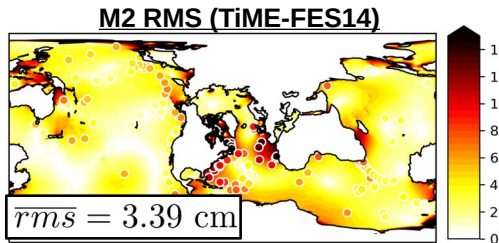
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Ocean Tide Model

We employ the ocean tide model TIME (Sulzbach, 2021)



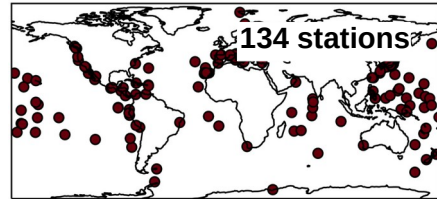
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Validation with TG-data (M. Hart-Davis)

- Tidal analysis of tide gauge data (GESLA) to TICON-dataset (open ocean subset) (Piccioni, 2019)
- TG-constituents represent **point measurements**

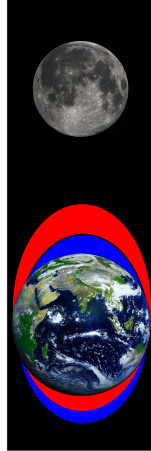


Barotropic Ocean Tide Modeling and Validation

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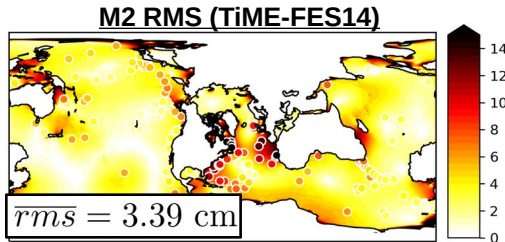
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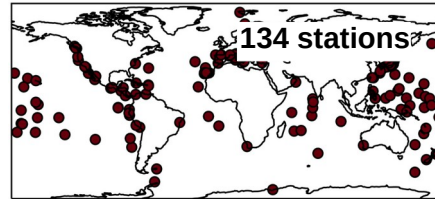
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Validation with SG-data (H. Wziontek)

- Tidal analysis of superconducting gravimeter time-series with ETERNA-X (<http://ggp.bkg.bund.de/eterna>)
- Modeling of surface gravimetric signals with spotl (Agnew, 2012)
- SG-constituents represent a **globally-integrated measurement**



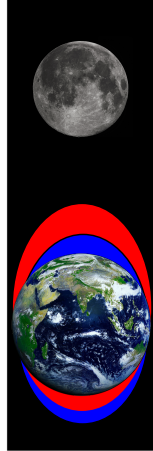
(OSG-030, Wettzell, Germany)

Barotropic Ocean Tide Modeling and Validation

MODELING

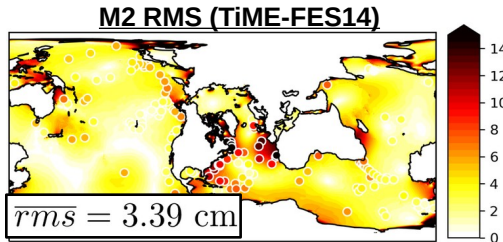
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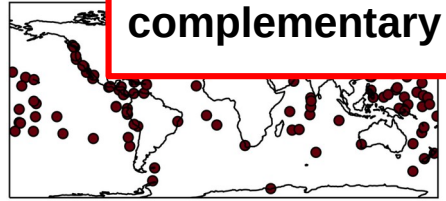
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→ **SG and TG data represent complementary tidal metrics**

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- SG-constituents represent a **globally-integrated measurement**



(OSG-030, Wettzell, Germany)

Data-unconstrained Degree-3 Tidal Atlas

- We employ the nomenclature of Ducarme (2012) for labeling partial tides
→ monthly species (**3MO0**), diurnal species (**M1**), semidiurnal species (**3MO2, 3MK2**),
terdirunal species (**M3**)

- We employ the **root-mean-square** metric to compare modeled vs. analyzed constituents

$$rms(\zeta_M^\omega) = \sqrt{\frac{1}{2 \cdot 134} \sum_{i=1}^{134} |\zeta_M^\omega(\mathbf{x}_i) - \zeta_{TG}^\omega(\mathbf{x}_i)|^2} \quad rms(g_M^\omega) = \sqrt{\frac{1}{2 \cdot 16} \sum_{i=1}^{16} |g_M^\omega(\mathbf{x}_i) - g_{SG}^\omega(\mathbf{x}_i)|^2}$$

- TiME-solutions correspond closely to recently published studies:

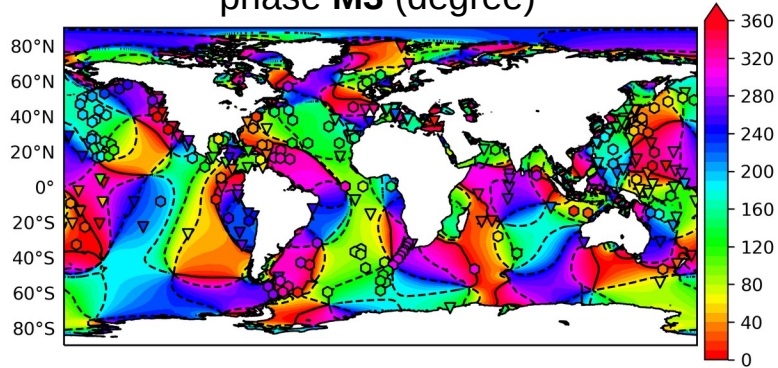
→ Data-unconstrained solution for M1 (Woodworth, 2019)

→ Altimetry data-constrained atlas for M1, 3MO2, 3MK2, M3 (Ray, 2020)

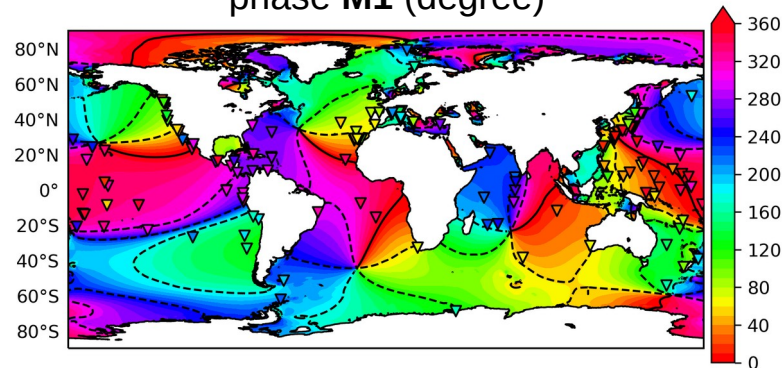
TG-rms is minimized by varying model parameters

Modeled and Analyzed Sea Level Signal

phase M3 (degree)



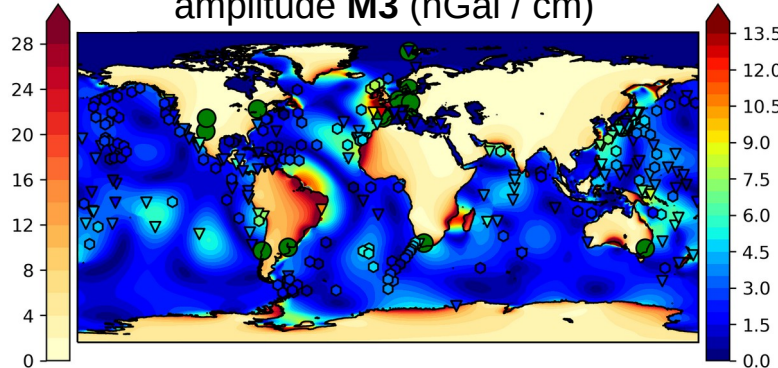
phase M1 (degree)



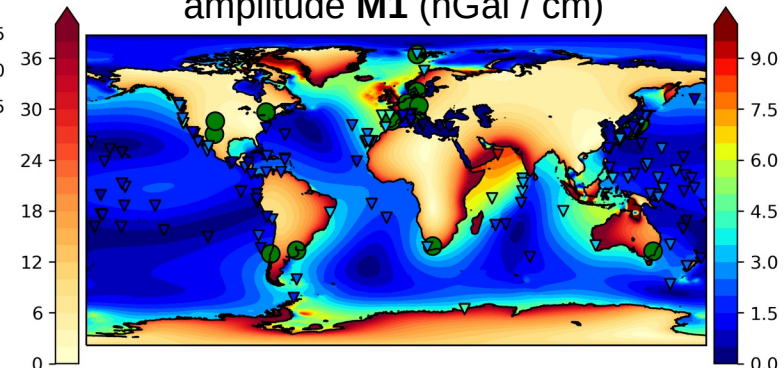
3MO2

0.9 / 2.5 mm

amplitude M3 (nGal / cm)



amplitude M1 (nGal / cm)



3MK2

0.9 / 2.0 mm

Mean agreement
between **33%** (M1)
and **64%** (3MO2)

rms/signal :

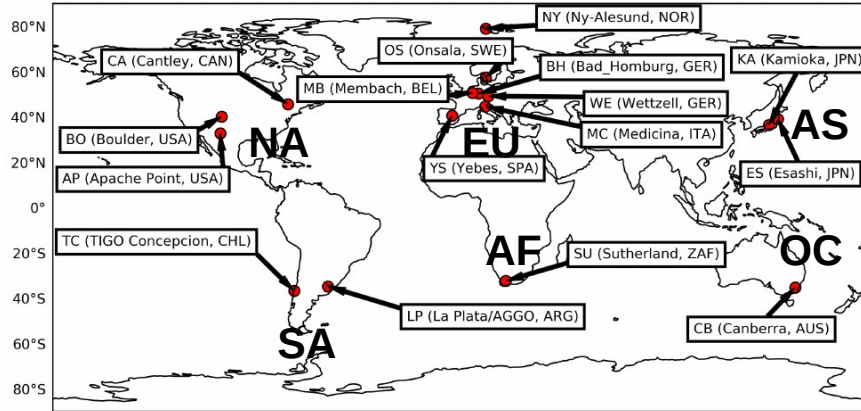
M3 1.3 / 2.9 mm

M1 1.0 / 1.5 mm

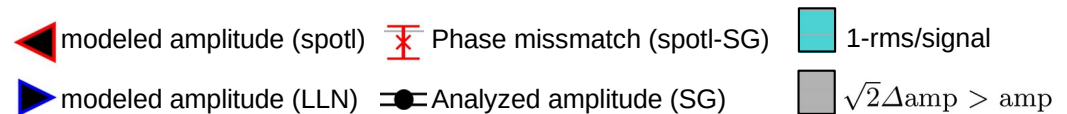
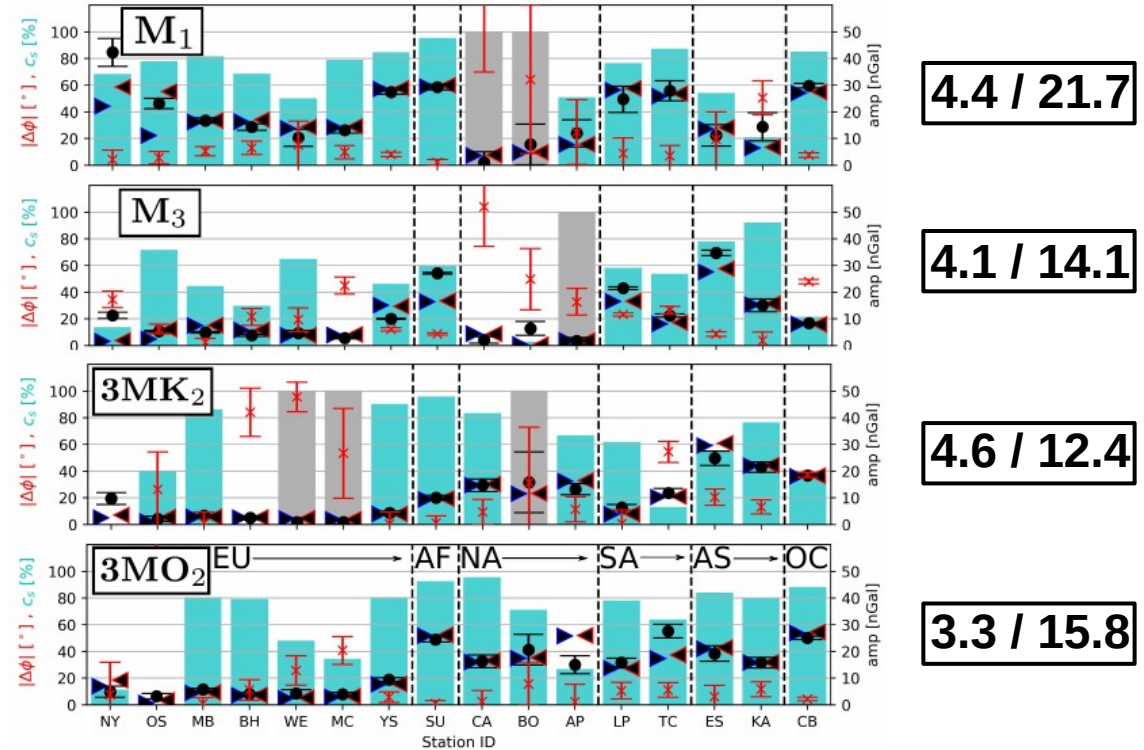
Modeled and Analyzed Gravimetric Signal

rms/signal [nGal]

Global SG-distribution













- Global ensemble of 16 SG stations
- Mean agreement between **63%** (3MK2) and **80%** (M1)



Summary

- First data-unconstrained tidal atlas comprising partial tides of all degree-3 tidal species
- Tidal analysis of SG time series feasible for few nGal degree-3 signals with ETERNA-x
- Rms-metric for tide gauge and SG ensemble shows agreement over 50%
→ Modeled and analyzed tidal signals correspond to each other
- The mean gravimetric signal is highest for diurnal and long-period tides (M1, 3MO0), while the respective tide gauge signals are small
→ SG data is especially useful to validate small-amplitude tides with relatively long periods

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