

RECEIVED: March 28, 2014

REVISED: May 21, 2014

ACCEPTED: June 4, 2014

PUBLISHED: June 27, 2014

Majorana dark matter with a coloured mediator: collider vs direct and indirect searches

Mathias Garny,^a Alejandro Ibarra,^b Sara Rydbeck^c and Stefan Vogl^b

^a*CERN Theory division,
CH-1211 Geneva 23, Switzerland*

^b*Physik-Department T30d, Technische Universität München,
James-Frank-Straße, 85748 Garching, Germany*

^c*Deutsches Elektronen-Synchrotron DESY,
Notkestraße 85, 22603 Hamburg, Germany*

E-mail: mathias.garny@cern.ch, ibarra@tum.de, sara.rydbeck@desy.de,
stefan.vogl@tum.de

ABSTRACT: We investigate the signatures at the Large Hadron Collider of a minimal model where the dark matter particle is a Majorana fermion that couples to the Standard Model via one or several coloured mediators. We emphasize the importance of the production channel of coloured scalars through the exchange of a dark matter particle in the t-channel, and perform a dedicated analysis of searches for jets and missing energy for this model. We find that the collider constraints are highly competitive compared to direct detection, and can even be considerably stronger over a wide range of parameters. We also discuss the complementarity with searches for spectral features at gamma-ray telescopes and comment on the possibility of several coloured mediators, which is further constrained by flavour observables.

KEYWORDS: Beyond Standard Model, Cosmology of Theories beyond the SM

ARXIV EPRINT: [1403.4634](https://arxiv.org/abs/1403.4634)

Contents

1	Introduction	1
2	Particle physics model and observables	3
2.1	Thermal relic density	4
2.2	Indirect detection	5
2.3	Direct detection	6
2.4	Production at LHC	7
3	Re-interpretation of LHC constraints	10
4	Results	12
4.1	Comparison with direct detection	14
4.2	Comparison with indirect detection	14
4.3	Exclusion for a thermal relic	17
5	Conclusions	18
A	Flavour constraints	19

1 Introduction

Despite the mounting evidence for the existence of dark matter (DM) in galaxies, clusters of galaxies and the Universe at large scale, the nature and properties of the dark matter particle are still largely unconstrained by observations. In fact, viable dark matter models have been constructed with masses ranging between $\sim 1 \mu\text{eV}$ and $\sim 10^{16} \text{ GeV}$, and interaction cross sections ranging between $\sim 10^{-35} \text{ pb}$ and $\sim 1 \text{ pb}$ (for a review, see [1]). In this vast parameter space of dark matter models, Weakly Interacting Massive Particles (WIMPs) still stand as one of the most promising dark matter candidates, since for reasonable values of the model parameters, the freeze-out of dark matter WIMPs from the thermal plasma left a relic population with an abundance which reproduces qualitatively well the measured value of the dark matter density $\Omega_{\text{DM}} h^2 = 0.1199 \pm 0.0027$ [2].

There are presently three different approaches pursued in order to detect the non-gravitational effects of WIMPs with ordinary matter: direct detection, indirect detection and collider experiments. This decade is being especially prolific in experimental results in the three search strategies. Indeed, various experiments currently in operation are setting strong limits on the WIMP parameter space and ruling out regions where a dark matter signal could be expected, notably XENON100 [3] and LUX [4] in direct searches, Fermi-LAT [5], AMS-02 [6], H.E.S.S. [7], MAGIC [8], IceCube [9] in indirect searches and the LHC in collider searches (see e.g. [10–13]). Moreover, in the near future the 14 TeV run of

LHC, the XENON1T [14] and LZ [15] experiments, and the Cerenkov Telescope Array [16] will significantly improve the reach of collider, direct and indirect dark matter searches, respectively.

These three different approaches constrain the parameter space of dark matter models in a complementary way, however, the synergy of the various search strategies is very model dependent. In this paper we focus on a simple scenario where the dark matter particle is a Majorana fermion that couples to light quarks and a coloured scalar via a Yukawa coupling. This scenario, despite its simplicity, offers a very rich phenomenology in direct detection [17–19], indirect detection [20–25] and collider experiments [26–30]. In particular, when the mediator mass is comparable to the dark matter mass, this model predicts a sharp and relatively intense gamma-ray spectral feature which, if observed, would constitute an unambiguous signal for dark matter annihilations [31–33]. Additionally, the collider phenomenology is distinct from the widely-used effective operator approach (see e.g. [34–39]), because the mediator can be directly produced in proton proton collisions. Similar models, but with leptonic mediators, were studied in [22, 23, 40–45].

In this paper we focus on the collider constraints on this scenario. Recent analyses have remarked that colored scalars can be produced not only via the strong interactions but also via the exchange of a dark matter particle in the t-channel. Since the dark matter thermal production requires the Yukawa coupling to be sizeable, the latter production channel can be important or even dominant. The limits on the model parameters and the complementarity between collider searches and direct detection experiments has been investigated in [23, 26–29], employing limits on simplified supersymmetric models which were derived by the CMS collaboration [46, 47] based on events with jets and missing energy as well as various further constraints.

Here we go beyond these analyses by performing a dedicated re-interpretation of collider searches which includes also jet matching, that is important when considering the quasi-degenerate mass spectrum, and takes into account the model-dependence of the efficiencies, i.e. the number of signal events that are expected in each signal region of the experimental search for a given production process and kinematical configuration. A similar method was recently employed in [48], focusing on Dirac dark matter. We analyse the limits on the Yukawa coupling using the latest ATLAS search for jets and missing transverse energy [11] and investigate the complementarity of the collider limits with those from direct and indirect dark matter searches. Furthermore we discuss various sources of experimental and theoretical uncertainties of collider limits and assess their impact on the exclusion power. Finally, we consider an extension of the model by two coloured scalars coupling to the up-type quarks and we study the impact of extending the scalar sector on the dark matter searches in view of the stringent limits from flavour violation.

The paper is organized as follows. In section 2, we introduce the simplified model and discuss its properties with respect to indirect, direct and collider searches. Section 3 explains some details of our collider analysis. Our results are discussed and compared to direct and indirect detection constraints in section 4, and we conclude in section 5. The appendix contains a brief discussion of flavour constraints.

2 Particle physics model and observables

We assume the dark matter particle χ to be a Majorana fermion which couples to the light quarks via a Yukawa interaction with coloured scalars η_i . The Lagrangian of the model can be written as

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_\chi + \mathcal{L}_\eta + \mathcal{L}_{\text{int}}, \quad (2.1)$$

where \mathcal{L}_{SM} denotes the Standard Model (SM) Lagrangian while \mathcal{L}_χ and \mathcal{L}_η are given by

$$\begin{aligned} \mathcal{L}_\chi &= \frac{1}{2} \bar{\chi}^c i \not{\partial} \chi - \frac{1}{2} m_\chi \bar{\chi}^c \chi, \text{ and} \\ \mathcal{L}_\eta &= (D_\mu \eta_i)^\dagger (D^\mu \eta_i) - m_{\eta_i}^2 \eta_i^\dagger \eta_i, \end{aligned} \quad (2.2)$$

where D_μ denotes the covariant derivative. On the other hand, \mathcal{L}_{int} contains the interactions between the SM quarks and the dark sector,

$$\mathcal{L}_{\text{int}} = -f_{ij} \bar{q}_{Ri} \chi \eta_j + \text{h.c.}, \quad (2.3)$$

where f_{ij} is a Yukawa coupling matrix, q_{Ri} denote the right-handed quark fields and summation over flavours i, j is implied. This Lagrangian generically leads to too large flavour changing neutral currents, hence some conditions must be imposed on the Yukawa couplings to fulfil the stringent constraints from flavour observables. In the following we consider two scenarios:

1. We consider a single scalar η that couples exclusively to the right-handed up quarks, with coupling strength f . Phenomenologically, and as shown in appendix A, the constraints on new physics from $D - \bar{D}$ mixing require the coupling of η to charm quarks to be suppressed by about two orders of magnitude relative to the coupling to up quarks. This suppression can be realized by requiring an ‘‘alignment’’ type set-up similar to the corresponding scenario for the squark sector in the MSSM, which can be realized by appropriate flavour symmetries at a high scale [49].
2. We consider a pair of mass degenerate scalars η_u and η_c which couple to right-handed up and charm quarks with a universal coupling $f_{ij} = \delta_{ij} f$. This scenario corresponds to a framework of minimal flavour violation [50] which requires flavour universality among quarks with the same gauge quantum numbers while allowing a separation of particles belonging to different multiplets. In this case, constraints from $D - \bar{D}$ mixing require the mass degeneracy of η_u and η_c to hold at the percent level, as shown in appendix A.

We also show explicitly in appendix A that the limits from flavour observables are satisfied even when the condition of alignment or the condition of universality are imposed at a high energy scale, close to the Planck or GUT scales. A completely analogous argument applies to scenarios where the dark matter particle couples to right-handed down-type quarks. However, for a coupling to left-handed quarks, more stringent limits would apply because the alignment cannot be implemented simultaneously in the up- and down-type sectors [51].

In the following we concentrate on the above two scenarios for definiteness. The model is thus completely described by the two masses m_χ and m_η of the dark matter and the mediator(s), respectively, and by the Yukawa coupling f . With this framework it is possible to calculate various dark matter observables, e.g. the relic density, the annihilation cross section, the dark matter-nucleon scattering cross section or event rates at the LHC, and compare their relative exclusion power.

An interesting particularity of the model analyzed here is that the strongest experimental constraints can not be derived from a small set of effective operators, but require to consider higher order effects. Concretely, for indirect detection the two-to-three and loop-induced annihilation channels play an important role, firstly because the leading order two-to-two channel is helicity and velocity suppressed, and second because the hard gamma-ray spectrum from $\chi\chi \rightarrow q\bar{q}\gamma$ and the loop induced processes $\chi\chi \rightarrow \gamma\gamma, \gamma Z$ generate a very distinct spectral signature [22, 23, 31, 32]. For direct detection, the lowest order operators mediating spin-independent interactions are suppressed for Majorana dark matter with chiral interactions, such that higher order contributions and the spin-dependent scattering have to be also considered [17, 18]. Lastly, the production at the LHC is governed not only by the strong processes, but also by processes mediated by the Yukawa interaction with the dark matter particle [26–29].

In the following, we summarize the relevant features of the model concerning the relic density, as well as the direct and indirect detection,¹ and then discuss in detail the signatures at the LHC.

2.1 Thermal relic density

Probably the most compelling argument for WIMP dark matter is that this class of particles is produced quite naturally in the early Universe and can generate, after thermal freeze-out, the correct relic density $\Omega_{\text{DM}}h^2 = 0.1199 \pm 0.0027$ [2] as measured by the Planck satellite. The Lagrangian (2.1) allows for tree level annihilations $\chi\chi \rightarrow q\bar{q}$ and in most of the parameter space the relic abundance is set by this process. However, for $m_\eta/m_\chi \lesssim 1.2$ the scalar η does not freeze-out before the dark matter particle χ and modifies the relic density [52]. This process, which is known as coannihilation, can be approximately taken into account by first defining an effective cross section

$$\sigma v_{\text{eff}} = \sigma v(\chi\chi) + \sigma v(\chi\eta)e^{-\frac{m_\eta - m_\chi}{T_{\text{fo}}}} + \sigma v(\eta\eta)e^{-\frac{2(m_\eta - m_\chi)}{T_{\text{fo}}}}, \quad (2.4)$$

where T_{fo} corresponds to the freeze-out temperature while $\sigma v(\chi\eta)$ and $\sigma v(\eta\eta)$ correspond to the thermally averaged annihilation cross-section of a $\chi\eta$ or an $\eta\eta$ pair respectively, and then replacing the thermally averaged cross section by this effective cross section in the well-known solution to the Boltzmann equation neglecting coannihilations. In our analysis, we use micrOMEGAs2.4 [53] to calculate the relic density in a full numerical approach (see also [54] for a recent discussion of Sommerfeld enhancement in a similar context).

¹A detailed discussion including expressions for the spin dependent (SD) and spin independent (SI) scattering cross section can be found in [18, 23].

2.2 Indirect detection

The processes relevant for dark matter annihilations in the galaxy today are closely related to those that determined the thermal freeze-out in the early Universe. However, the freeze-out took place when the dark matter particles were still relativistic while annihilations today are a non-relativistic phenomenon. Expanding the tree level annihilation cross section for the two-to-two process for small values of the relative center of mass velocity, v , one obtains [55]

$$(\sigma v)_{2\text{-body}} = \frac{3f^4}{32\pi m_\chi^2} \frac{m_q^2}{m_\chi^2} \frac{1}{(1+\mu)^2} + \mathcal{O}(v^2), \quad (2.5)$$

with $\mu = m_\eta^2/m_\chi^2$ and m_q the mass of the final state quark. Therefore, the tree level annihilation cross section for the two-to-two process is suppressed either by m_q^2/m_χ^2 , due to the helicity suppression,² or by the small velocity of the dark matter particles in the Galaxy today, $v \approx 10^{-3}$. As a result, higher order processes can potentially give the dominant contribution to the indirect detection signals.

In the model considered here two higher order processes become relevant. First, the loop induced annihilation into two gauge bosons $\chi\chi \rightarrow \gamma\gamma, \gamma Z, ZZ, WW, gg$ [25, 56–58], and second, the three-body annihilation $\chi\chi \rightarrow q\bar{q}V$ ($q\bar{q}h$), where a gauge boson V (Higgs boson h) is emitted in association with the quarks [20, 21, 31, 32, 40–42, 59–69]. These processes can dominate over the annihilation in $q\bar{q}$ pairs even though they are loop suppressed or three-body phase space suppressed, since they can generate velocity independent terms which do not suffer from helicity suppression. The analytical result for the cross sections into $\gamma\gamma$ and γZ is rather lengthy and we refer the reader to e.g. [56–58]. On the other hand, the total annihilation cross section into two massless quarks and one photon is approximately given by [32, 41]

$$(\sigma v)_{3\text{-body}} \simeq \frac{\alpha_{\text{em}} f^4 3Q_q^2}{64\pi^2 m_\chi^2} \left\{ (\mu+1) \left[\frac{\pi^2}{6} - \ln^2\left(\frac{\mu+1}{2\mu}\right) - 2\text{Li}_2\left(\frac{\mu+1}{2\mu}\right) \right] + \frac{4\mu+3}{\mu+1} + \frac{4\mu^2-3\mu-1}{2\mu} \ln\left(\frac{\mu-1}{\mu+1}\right) \right\}, \quad (2.6)$$

where Q_q is the electric charge of the quark.

Due to the excellent energy resolution and the high statistics of present gamma-ray observatories, such as the Fermi-LAT or H.E.S.S., the most notable indirect detection signature in this model is the hard gamma-ray spectral feature arising from the processes $\chi\chi \rightarrow \gamma\gamma$ and $\chi\chi \rightarrow q\bar{q}\gamma$ (the gamma-ray line from $\chi\chi \rightarrow \gamma Z$ is always subdominant). As $\chi\chi \rightarrow q\bar{q}\gamma$ scales like $1/\mu^4$ in the limit of large μ , while $\chi\chi \rightarrow \gamma\gamma$ only scales as $1/\mu^2$, the former process is most relevant for moderate values of $\mu \lesssim 4$. With current instruments the spectrum of internal bremsstrahlung is practically indistinguishable from a gamma-ray line, see figure 1, hence it is necessary to derive limits on the combined spectrum based on data used in line searches. In the following we use the same procedure

²It is interesting to remark that the helicity suppression can be relaxed for a mediator with a small flavour off-diagonal coupling f' to third-generation quarks, for which $\sigma v_{q\bar{q}'} \propto f^2 f'^2 \max(m_q^2, m_{q'}^2)$, contrary to the naive expectation $\propto f^2 f'^2 m_q m_{q'}$. However, we will not pursue this possibility further here.

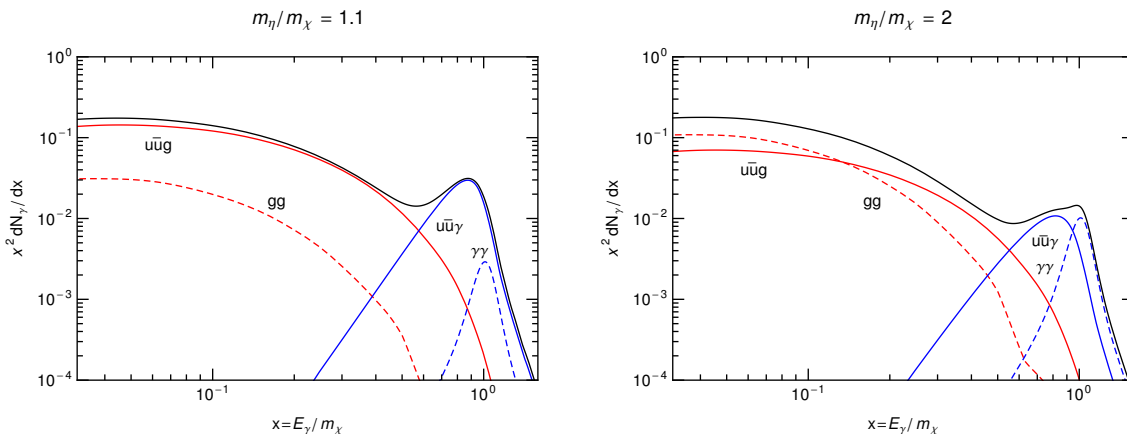


Figure 1. Energy spectrum of gamma rays produced in the annihilation channels $u\bar{u}\gamma$, $\gamma\gamma$ as well as $u\bar{u}g$ and gg convolved with the Fermi-LAT energy resolution, for $m_\chi = 100$ GeV, $m_\eta = 1.1m_\chi$ (left panel) and $m_\eta = 2m_\chi$ (right panel). The black line indicates the total spectrum. Note that for $u\bar{u}\gamma$ only the primary spectrum is shown. The secondary gamma rays from this channel are negligible compared to those arising from $u\bar{u}g$.

as in [23] and derive limits on the combined annihilation cross section into hard gamma-rays $\sigma v_{\text{combined}} = 2\sigma v_{\gamma\gamma} + \sigma v_{q\bar{q}\gamma}$ employing data from the Fermi-LAT [22] and H.E.S.S. [7] observations of the galactic center region.

2.3 Direct detection

The s-channel exchange of the scalar η between the dark matter χ and the quark induces spin dependent (SD) as well as spin independent (SI) scatterings off nucleons, while further contributions to the SI scattering arise from loop level interactions with both the quarks and the gluons [70]. On the one hand, the leading contribution to the SD interactions can be described by a dimension-six axial-vector dark matter quark interaction [71]

$$\mathcal{L}_{\text{eff}}^{\text{SD}} = d_q \bar{\chi} \gamma^\mu \gamma^5 \chi \bar{q} \gamma_\mu \gamma^5 q, \quad (2.7)$$

where the dark matter coupling to the quarks d_q is a dimensional parameter which scales as

$$d_q \propto \frac{f^2}{m_\eta^2 - (m_\chi + m_q)^2}. \quad (2.8)$$

The case of SI scattering is, on the other hand, more involved since the coefficient f_q of the scalar term in the effective Lagrangian $\mathcal{L}_{\text{eff,scalar}}^{\text{SI}} = f_q \bar{\chi} \chi \bar{q} q$ vanishes at dimension-six for chiral interactions, while the coefficient for the vector interactions $\bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu q$ vanishes to all orders, due to χ being a Majorana fermion. Consequently the leading contribution to the SI coupling between the dark matter and the nucleons is generated at higher order. Expanding the scalar exchange beyond dimension six, the first non vanishing contribution arises at dimension eight [71]; the strength of this interaction is proportional to

$$g_q \propto \frac{f^2}{(m_\eta^2 - (m_\chi + m_q)^2)^2}. \quad (2.9)$$

A further, subdominant, contribution to the dark matter nucleus coupling is induced by the scattering of the dark matter off the gluon content of the nucleon via a scalar-quark loop, which generates a dimension-seven effective operator [71].

Due to the structure of d_q and g_q , a small mass difference $\Delta m = m_\eta - m_\chi$ between the scalar particle η and the dark matter particle χ can lead to a drastic enhancement of both the SD and SI scattering cross sections [17, 18, 72] (see [73] for a recent discussion of coupling to b-quarks). Since the SI scattering is generated by a higher order operator than the SD scattering cross section, the SD dark matter-proton cross section σ_p^{SD} can exceed the SI dark matter-proton cross section σ_p^{SI} by a factor $\sim 10^2$ – 10^8 at $m_\eta/m_\chi = 1.1$. However, since direct detection experiments are less sensitive to the SD scattering, the strongest constraints on the model parameters do not necessarily arise from the experimental limits on the SD interactions.

In our analysis we consider constraints from two different experiments, LUX [4] and XENON100 [3]. In the case of LUX we compare our theoretical prediction for the SI dark matter proton scattering cross section σ_p^{SI} directly with the limits published by the collaboration, while for XENON100 we use the same procedure as in [18] and derive the limit from the total scattering rate, i.e. including both SD and SI contributions.³ Note that SIMPLE and COUPP [74, 75] yield comparable constraints for cases where the SD part dominates, since the scattering cross section off neutrons and protons is comparable for the model considered here.

2.4 Production at LHC

Searching for dark matter at the LHC is inherently difficult as the production of particles which do not trigger a signal at the detectors can only be investigated through the observation of large amounts of missing transverse energy (MET). In the recent past, mono-jet events with large MET have been a popular method to derive limits on the dark matter interactions with the SM particles [36, 37]. However in models such as the one considered here it is possible to probe the dark sector more efficiently by searching for the production of the mediator η instead of the dark matter particle χ . As η is unstable and decays into a χq pair, the expected signature of $\eta\bar{\eta}$ ($\eta\eta$) production are n -jet events, $n \geq 2$, with large missing energy, which allows for a better subtraction of the SM backgrounds than mono-jet events and consequently possess a higher sensitivity to new physics effects. Furthermore, since the mediator η is coloured, it can be copiously produced in proton-proton collisions through strong interactions.

There are three main production modes of η which need to be considered in a collider analysis. The first process is the production of $\eta\bar{\eta}$ pairs by the strong gauge interactions from gg or $q\bar{q}$ initial states, see figure 2 for the Feynman diagrams contributing to this process. The strong production cross section is set exclusively by the mass of η and depends neither on m_χ nor on the Yukawa coupling f . As can be seen in figure 3, due to the large gluon luminosity, the largest cross section arises from the gg initial state

³The LUX collaboration has not published limits on the total scattering rate, but derived their SI limits employing a full likelihood analysis of the recoil events, hence the approach in [18] cannot be applied to this case.

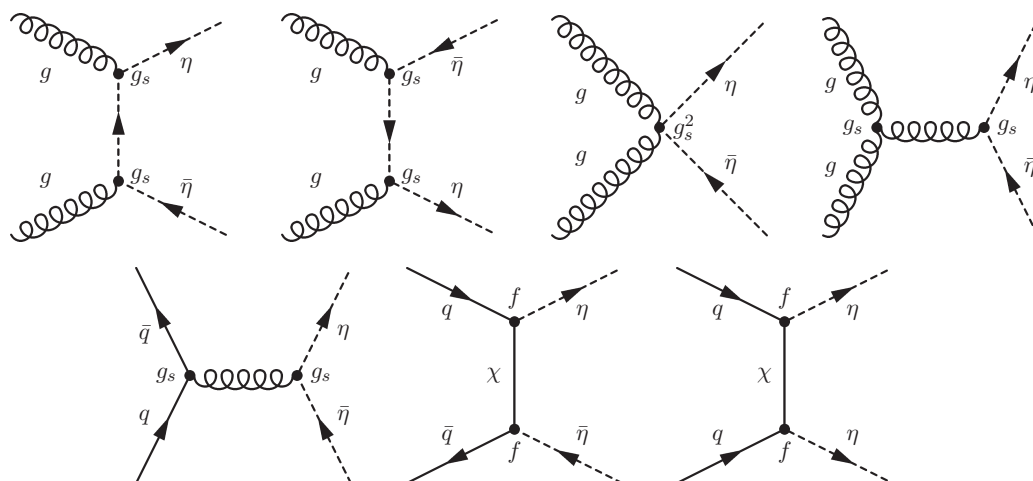


Figure 2. Feynman diagrams contributing to the production of coloured scalar mediators at a hadron collider.

with $u\bar{u}$ and $d\bar{d}$ contributing at the $\mathcal{O}(1 - 10\%)$ level, while other quark flavours can be neglected. A second contribution is the production of $\eta\bar{\eta}$ from the $u\bar{u}$ initial state with a dark matter particle χ in the t-channel. This process is not independent but can interfere with the QCD contribution, see figure 2. For small values of f the cross section is largely dominated by the QCD processes, however for a moderate Yukawa coupling, $f \approx 0.5$, these two contributions are of similar strength and interfere destructively, thus leading to a slight decrease of the cross section (see figure 3, left panel), while for larger values of f the t-channel exchange begins to dominate and the cross section increases with f^4 . The third contribution, $\eta\eta$ pair production, can not be induced by gauge interactions and is entirely due to the exchange of a dark matter particle in the t-channel. This process, which is similar to squark pair production from gaugino exchange in the MSSM, requires a chirality flip of the t-channel fermion and is thus proportional to the squared mass of the dark matter particle m_χ^2 . Therefore the cross section $\sigma(\eta\eta)$ decreases with the DM mass and disappears in the limit of a vanishing Majorana mass, whereas $\sigma(\eta\bar{\eta})$ increases slightly with lower m_χ since the t-channel exchange gets less suppressed by the mass in the propagator, as apparent from figure 3, right panel. Since the parton distribution function for the up quark is significantly larger than for the anti-up quark, the cross section $\sigma(\eta\eta)$ receives a considerable enhancement relative to $\sigma(\eta\bar{\eta})$ and dominates the total cross section in large regions of the parameter space (see also [76] for a similar effect related to gluino exchange).

Leading order calculations at the LHC are subject to large corrections from next to leading order (NLO) effects. While a full computation of the NLO corrected cross section σ^{NLO} is beyond the scope of this work, one can estimate its value using the well-known results from supersymmetric scenarios. Let us consider first the corrections to the partonic processes which do not receive a contribution from fermion t-channel exchange, namely $gg \rightarrow \eta\bar{\eta}$ and $dd \rightarrow \eta\bar{\eta}$. This case is completely analogous to the squark production in simplified supersymmetric models where all SUSY particles, except for the light squarks,

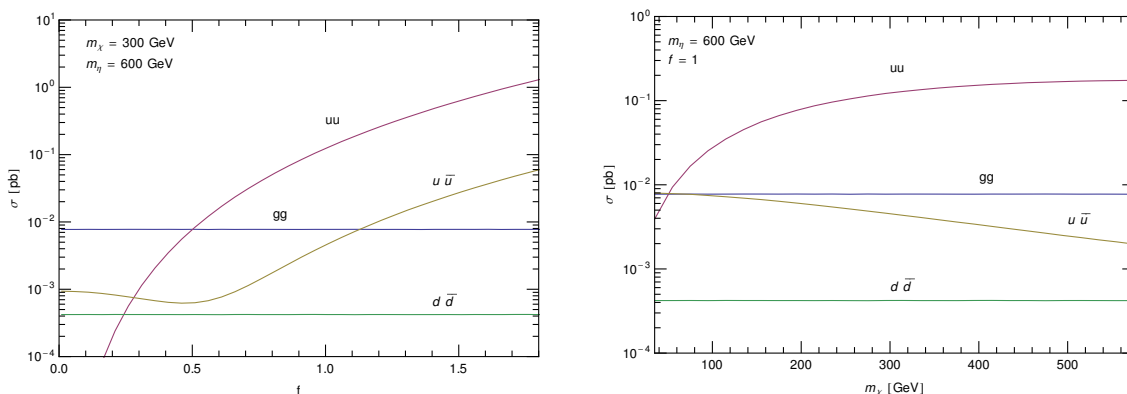


Figure 3. Contributions to the production cross section of the mediator η in proton-proton collisions with center of mass energy of 8 TeV as a function of the coupling f for $m_\chi = 300$ GeV and $m_\eta = 600$ GeV (left panel) and as a function of the dark matter mass for fixed coupling $f = 1$ and $m_\eta = 600$ GeV (right panel).

are assumed to be decoupled. For this case, the cross section is available at NLO and taking the resummation of next to leading logarithms (NLL) into account, $\sigma_{\text{QCD}}^{\text{NLO+NLL}}$ [77]. In the following we use the value from [78]. On the other hand, there is no calculation available of the NLO corrections to the channels $uu \rightarrow \eta\eta$ and $u\bar{u} \rightarrow \eta\bar{\eta}$, where in addition to the strong production there is a contribution from the exchange of a dark matter particle in the t-channel. For these processes, we therefore use the leading-order cross section as fiducial value and assume as an estimate for the maximal size the value reported in [79] for the NLO correction to the squark-squark pair production due to the exchange of a gluino in the t-channel, $K \approx 1.4$. We stress that in our toy model the exchanged fermion in the t-channel is a colour singlet and not a colour octet, and therefore this value should be considered only as indicative of the impact of the NLO corrections.

In order to incorporate the effects of the NLO corrections to the total production cross section we parametrize the full cross section as

$$\sigma = \sigma_{\text{QCD}}^{\text{NLO+NLL}} + K \times (\sigma^{\text{LO}}(f) - \sigma^{\text{LO}}(0)), \quad (2.10)$$

where $\sigma^{\text{LO}}(f)$ denotes the leading-order cross section for a given coupling f , namely $\sigma^{\text{LO}}(0)$ is the LO QCD contribution. We compute the LO using CalcHEP3.2 [80] with the CTEQ6 PDF set [81]. To estimate the uncertainty, we vary $\sigma_{\text{QCD}}^{\text{NLO+NLL}}$ within the theoretical error given in [77, 78] and the K -factor within the range 0.8–1.3, taking $K = 1$ as fiducial value; a rigorous treatment of the uncertainties related to NLO effects is beyond the scope of this paper. Finally, since QCD-mediated processes do not necessarily dominate the production of η , we performed a full Monte Carlo simulation of production and detector response in order to re-interpret experimental searches for simplified SUSY models within the scenario considered in this work.

3 Re-interpretation of LHC constraints

In order to derive collider constraints, we use the ATLAS search [11] for jets and missing transverse energy, based on $\mathcal{L} = 20.3 \text{ fb}^{-1}$ of data collected at a center of mass energy of 8 TeV. The search requires missing transverse energy $E_T^{\text{miss}} > 160 \text{ GeV}$, and transverse momentum $p_T > 130 \text{ GeV}$ for the leading jet, as well as $p_T > 60 \text{ GeV}$ for subleading jets. The search is divided into various signal regions characterized by the number of hard jets (ranging from two to six), as well as a number of further cuts, that are designed to suppress backgrounds (mainly diboson, Z/W+jets and $t\bar{t}$) as specified in [11]. The systematic uncertainties in the background rates are calibrated against four control regions.

The search does not find a significant excess above backgrounds and therefore presents 95% C.L. upper limits S_{95}^{obs} on the number of signal events in each signal region. For a given model, these are related to the upper limit on the production cross section σ via

$$S_{95}^{\text{obs}} = \sigma_{\text{vis}} \times \mathcal{L} = \sigma \times \epsilon \times \mathcal{L} , \quad (3.1)$$

where $\sigma_{\text{vis}} = \sigma \times \epsilon$ is the visible cross section, and the efficiency $\epsilon = N_{\text{after cuts}}/N_{\text{generated}}$ gives the fraction of the number of events passing all cuts required by a given signal region.

While the upper limits on the number of signal events in each signal region are model-independent, their interpretation in terms of simplified supersymmetric models relies on the corresponding efficiencies, which are model-dependent. For a large portion of the parameter space, the most relevant production channel is $uu \rightarrow \eta\eta$, different from the simplified supersymmetric model considered in [11]. Furthermore, for moderate mass splittings $m_\eta - m_\chi \lesssim \mathcal{O}(10^2 \text{ GeV})$ additional hard jets emitted either from the initial state, the final state or an intermediate particle in the diagrams shown in figure 2 contribute significantly to the visible cross section. Potentially, this introduces a further source of model-dependence.

Therefore, we determined the appropriate efficiencies for the model discussed in the previous section by generating a large number of events using MadGraph5 [82] interfaced with the detector simulation Delphes (version 3.0.10) [83]. Furthermore, we generate hard events with up to two additional partons in the final state. The potential double-counting with initial- and final-state radiation generated in the hadronization process (for which we use Pythia8 [84]) is taken into account by employing the MLM matching scheme, taking the minimum kt jet measure between partons to be $\text{xqcut} = m_\eta/4$ and the jet measure cutoff used by Pythia $\text{QCUT} = \text{xqcut}$. We validated the analysis by considering the simplified supersymmetric model with squark and neutralino and reproduced the cut-flow reported in [11] for the corresponding benchmark points (we typically find agreement at the sub-10% level, ranging up to 30% at most).

We compute the efficiencies for all signal regions containing up to four jets by generating a large number of events in a two-dimensional grid of parameter points for $m_\chi, m_\eta/m_\chi$, while setting the coupling $f = f_{\text{th}}(m_\eta, m_\chi)$ to the value expected for a thermal relic. For each point in parameter space, we then derive an upper limit on the production cross section via eq. (3.1). We select the signal region with the best expected sensitivity $\epsilon \times S_{95}^{\text{exp}}$, where the latter are taken from [11]. The computation of efficiencies can be affected by uncertainties related to the matching procedure. To estimate this uncertainty we varied

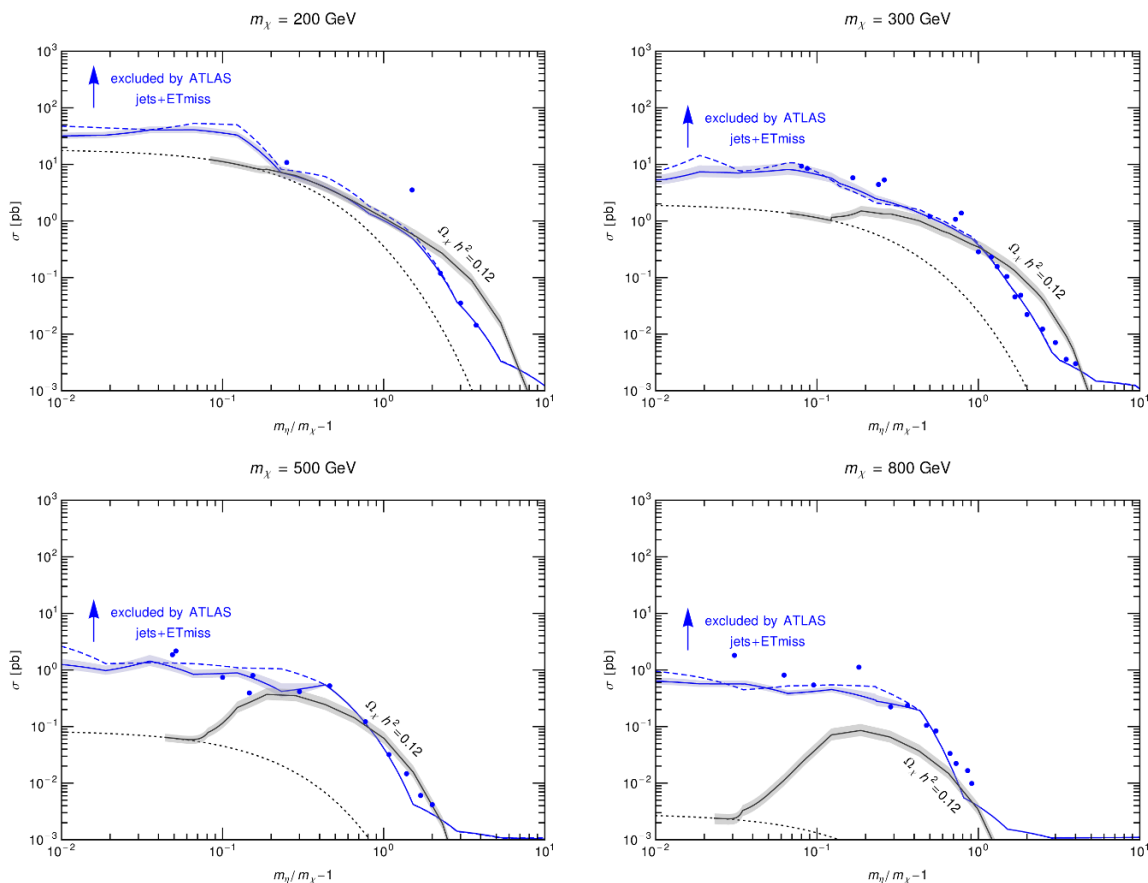


Figure 4. Upper limit on the production cross section from the ATLAS search [11] for jets and missing transverse energy (blue) as a function of the mass splitting between the dark matter and mediator particle. The four panels correspond to $m_\chi = 200, 300, 500, 800$ GeV. The black line shows the expected cross section for a thermal WIMP. The black dotted line is the production cross section arising from QCD interactions only (i.e. for $f \rightarrow 0$). The blue dashed line corresponds to the limit one would obtain when including only one additional ISR/FSR jet in the matching. For comparison, the blue dots mark the upper limit given by ATLAS [11] for a simplified supersymmetric model containing squarks and neutralino.

the matching scales x_{qcut} and Q_{CUT} within a range of a factor of two, and find changes in the efficiencies below $\sim 30\%$. In addition, the efficiencies can be affected considerably by statistical uncertainties related to the finite number of generated events. This is critical in particular for very small masses m_χ and small splittings m_η/m_χ , and for the signal regions containing three or four jets. In order to reduce this uncertainty as far as possible, we used up to $N_{\text{generated}} \simeq 1.2 \cdot 10^6$ events. Nevertheless, for a given set of masses, we exclude all signal regions for which the statistical 1σ error of the efficiency is above 30%. The corresponding uncertainty of the upper limit on the production cross section is shown as blue band in figure 4.

4 Results

In this section we present and discuss our main results obtained from re-interpreting the ATLAS search [11] for jets and missing transverse energy for the dark matter model described in section 2, and compare the resulting constraints to those from direct and indirect searches. We mostly focus on the case of a single coloured mediator that couples to the u_R quark for definiteness, but also consider the case of two mass-degenerate mediators that couple to u_R and c_R , respectively.

As expected, the upper limit that can be placed on the production cross section depends strongly on the mass splitting $\delta \equiv m_\eta/m_\chi - 1$ between the mediator η and the dark matter particle χ , see figure 4. For $\delta \gg 1$, cross sections down to ~ 1 fb can be excluded, the most sensitive signal regions being those with three and four jet final states (more precisely Bt and Ct in the notation of [11]) due to a better background suppression. At intermediate splittings $\delta \sim \mathcal{O}(1)$, the limit weakens by several orders of magnitude due to a loss in efficiency. Here the signal regions with looser requirements, i.e. more statistics, tend to become more important (Bm and Cm). For very small mass splittings $\delta \ll 1$, the limit on the cross section reaches a plateau at 0.5–50 pb, depending on the mass. For small splittings the signal regions with two jets become important (Al and Am). This is due to a loss of efficiency in the ≥ 3 -jet signal regions, since the jets produced in the decay $\eta \rightarrow \chi q$ become too soft. Instead, the dominant contribution comes from additional hard jets radiated from initial, final or intermediate states. Consequently, when one would include only one additional jet in the matrix elements (our default is two), the exclusion limits would be weakened in this regime (blue dashed lines in figure 4).

For comparison, we also show the production cross section that is expected for a thermal relic in figure 4 (black lines). The black dotted line is the contribution mediated by the strong interaction (first five diagrams in figure 2). The additional production channel via t-channel exchange of χ (last two diagrams in figure 2) typically yields the dominant contribution (especially $uu \rightarrow \eta\eta$) for mass splitting $\delta \gtrsim 0.1$. In general, their size depends on the coupling f . For obtaining the black line in figure 4, f has been fixed by the requirement of producing the observed dark matter abundance via thermal freeze-out. For small mass splittings $\delta \lesssim 0.1$, coannihilation channels are important, such that rather small values of f are sufficient to obtain the observed abundance. In turn, this means that the expected production cross section is suppressed in this regime. The grey band in figure 4 indicates the estimated uncertainty of the production cross section as discussed in section 2.4.

Instead of fixing the coupling f , one may also treat it as a free parameter and determine an upper limit by requiring that the production cross section remains below the experimental upper limit. As can be seen in figure 5, the largest allowed values of f are of $\mathcal{O}(1)$ for $\delta \lesssim 2$ –3, and quickly grow for larger splittings. The blue dotted lines in figure 5 are obtained by varying both the exclusion cross section as well as the production cross section within the uncertainty ranges discussed in section 3 and section 2.4, respectively. Note that, whenever the QCD contribution to the production lies above the exclusion limit on its own, the upper limit on the coupling f formally approaches zero. This means that this set of masses is excluded independently of the value of f .

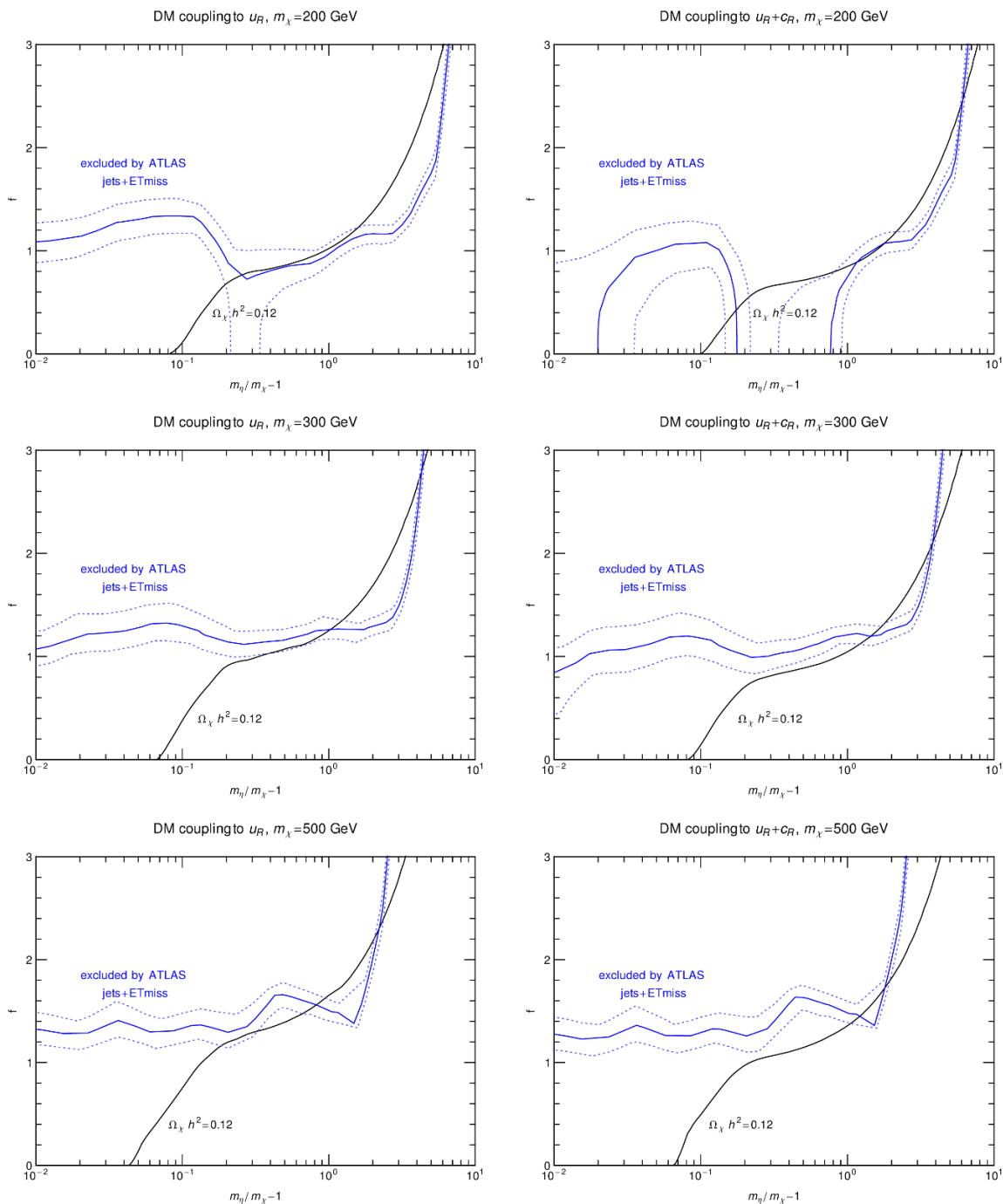


Figure 5. Upper limit on the coupling f inferred from the ATLAS search [11] for jets and missing transverse energy (blue) as a function of the mass splitting between the dark matter and mediator particle, for $m_{\chi} = 200, 300, 500$ GeV. The left panel corresponds to the case of a single mediator coupling to u_R , and the right to two mass-degenerate mediators coupling to u_R and c_R , respectively. The blue dotted lines indicate the uncertainty (see text for details), and the black line corresponds to a thermally produced WIMP.

The left panel of figure 5 shows the case of a single mediator that couples to u_R , and the right panel corresponds to two mediators coupling to u_R and c_R . The constraints are comparable, and the largest differences arise for small dark matter masses $m_\chi \lesssim 200$ GeV. The reason is that, in this region, the contribution to the production cross section arising from gluon initial states is important. This contribution doubles when considering two mediators, because it is flavour-insensitive. On the other hand, the production cross section is affected very little for the channels that depend on f , because these are typically dominated by $uu \rightarrow \eta\eta$. This explains why the corresponding limits are very similar to the case of a single mediator. However, the value of the coupling f required for producing the observed dark matter abundance via freeze-out is sensitive to the number N of mediators. Outside of the coannihilation region, $\Omega_\chi \propto N \times f^4$, i.e. $f_{\text{th}} \propto N^{-1/4}$ (for our numerical results we computed the relic density with micrOMEGAs in all cases, to take coannihilation effects into account).

4.1 Comparison with direct detection

The upper limits on the coupling f can be translated into limits on the spin independent and spin dependent scattering cross section.⁴ The corresponding constraints are shown in figure 6, together with upper limits from XENON100 [3, 85] and LUX [4]. For small mass splitting $\delta \ll 1$, the direct detection cross sections are resonantly enhanced, while the collider limits are weakened as discussed above. On the other hand, for $\delta = \mathcal{O}(1)$, the collider search is very effective, while the direct detection cross section is suppressed for Majorana dark matter with chiral couplings, as discussed in section 2.3. Consequently, when converted into the direct detection cross section, the ATLAS limits can be stronger by one to several orders of magnitude than current bounds from direct detection experiments for masses in the range $m_\chi = 10^2\text{--}10^3$ GeV. For masses around 100 GeV and $\delta = \mathcal{O}(1)$, the ATLAS constraint is strong enough to exclude even the QCD contribution to the production cross section at LHC. This translates into the dip in the constraint visible in the middle row of figure 6. Note, however, that while in general collider uncertainties only have a moderate impact, the upper limit is considerably affected in this range (see blue dotted lines in figure 6). For comparison, the ATLAS constraint for u_R/c_R mediators is also shown by the blue dashed lines in figure 6. The cross section expected for a thermal relic is also shown as black solid (dashed) line for u_R (u_R/c_R) mediators.

4.2 Comparison with indirect detection

One of the most interesting features of the dark matter model discussed here is the presence of a sharp spectral feature in the dark matter annihilation spectrum. It arises mainly from internal bremsstrahlung $\chi\chi \rightarrow q\bar{q}\gamma$ for $\delta \lesssim \mathcal{O}(1)$, while for $\delta \gtrsim \mathcal{O}(1)$, also the gamma-ray line resulting from the loop-induced process $\chi\chi \rightarrow \gamma\gamma$ gives a significant contribution. In figure 7, we compare constraints on $\sigma v_{q\bar{q}\gamma} + 2\sigma v_{\gamma\gamma}$ from gamma-ray observations of the

⁴Note that this translation depends on the nuclear parameters entering the SI and SD scattering cross section [70]. Within the model considered here, the SI scattering cross section is particularly sensitive to the second moments of the parton distribution function $q(2)$. The range of uncertainties discussed in [18] implies an uncertainty of the collider limits of up to 50%, when translated into direct detection cross sections. For the results shown in figure 6 we used the fiducial values as specified in [18].

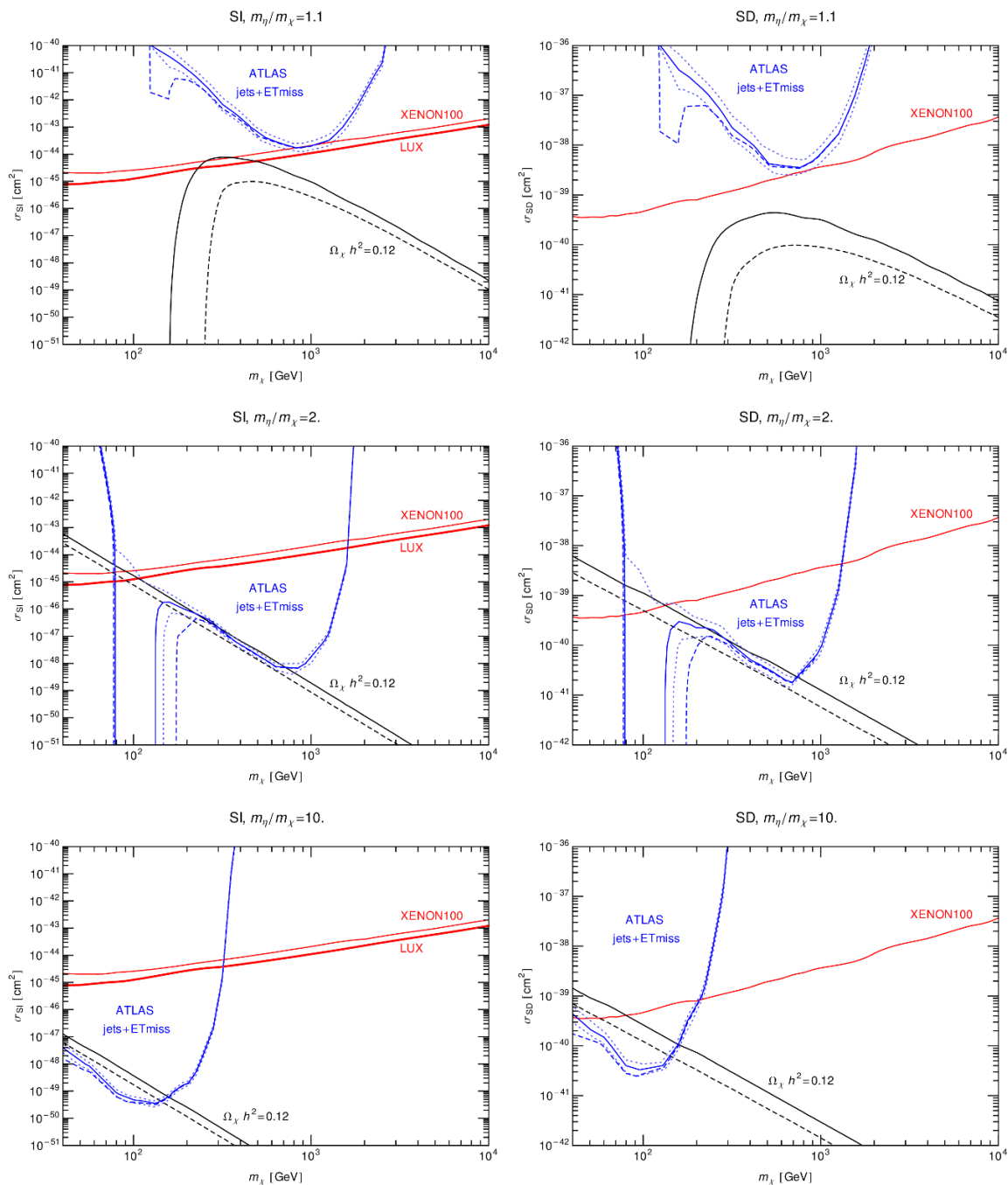


Figure 6. Comparison of constraints inferred from the ATLAS search [11] for jets and missing energy with the spin independent (-dependent) scattering cross section off protons (neutrons), shown in the left (right) panel. The rows correspond to mass ratios $m_\eta/m_\chi = 1.1, 2, 10$ between the dark matter and mediator mass. Solid lines correspond to the case where dark matter couples to u_R , and dashed where it also couples to c_R . The blue dotted lines indicate the uncertainty of the collider constraint for the case of u_R -coupling (see text for details).

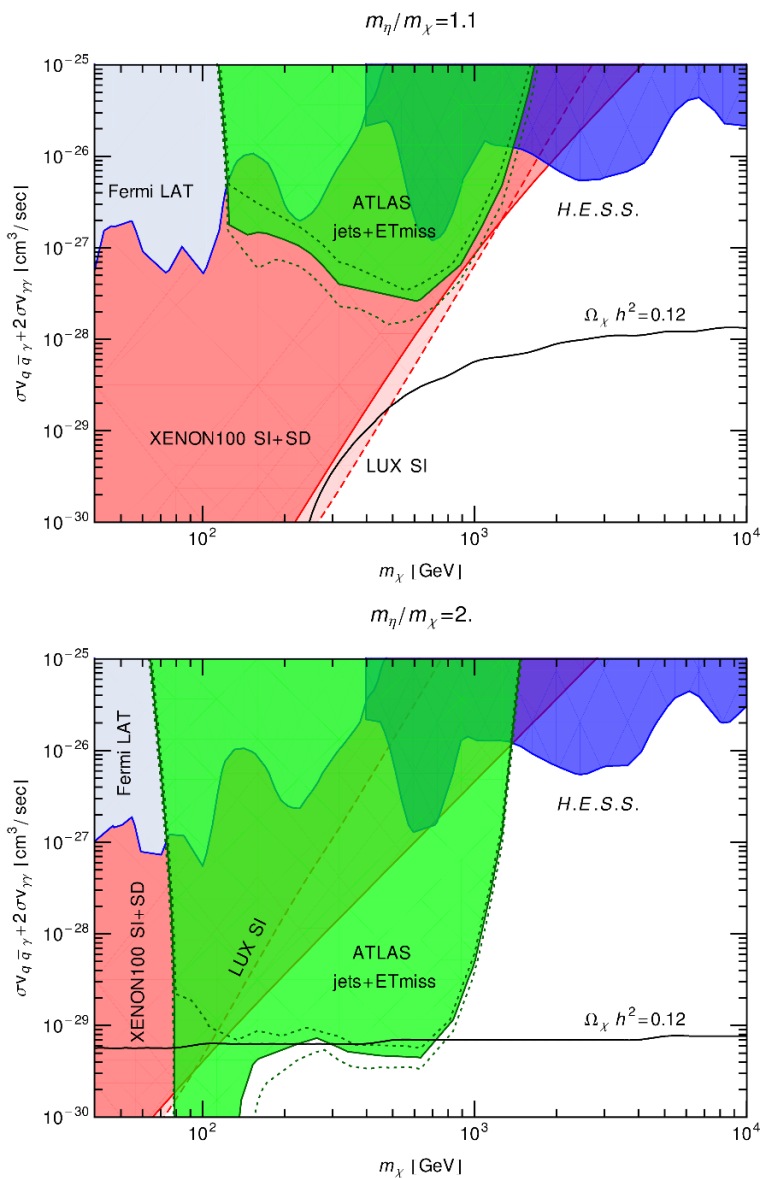


Figure 7. Comparison of constraints on the annihilation cross section obtained from searches for spectral features by the Fermi-LAT [22] and H.E.S.S. [7] (cf. [23]), with constraints inferred from collider searches for jets and missing energy by ATLAS [11], as well as direct detection limits from XENON100 [3] and LUX [4]. The black line corresponds to a thermal WIMP, and the dotted lines indicate the uncertainty of the collider constraint, as discussed before. Note that the results for u_R/c_R mediator are very similar, and are therefore not shown.

central galactic halo by Fermi-LAT [22] and H.E.S.S. [7] (blue shaded regions) with those inferred from direct detection [23] and from the ATLAS search [11] considered here. As expected, for small mass splitting, the region excluded by the LHC search (green region) is less constraining than XENON100 and LUX (red region). However, for mass splitting of order one, the ATLAS search severely constrains the possibility to observe a spectral feature arising from dark matter with a coloured mediator below $\mathcal{O}(1)$ TeV energies.

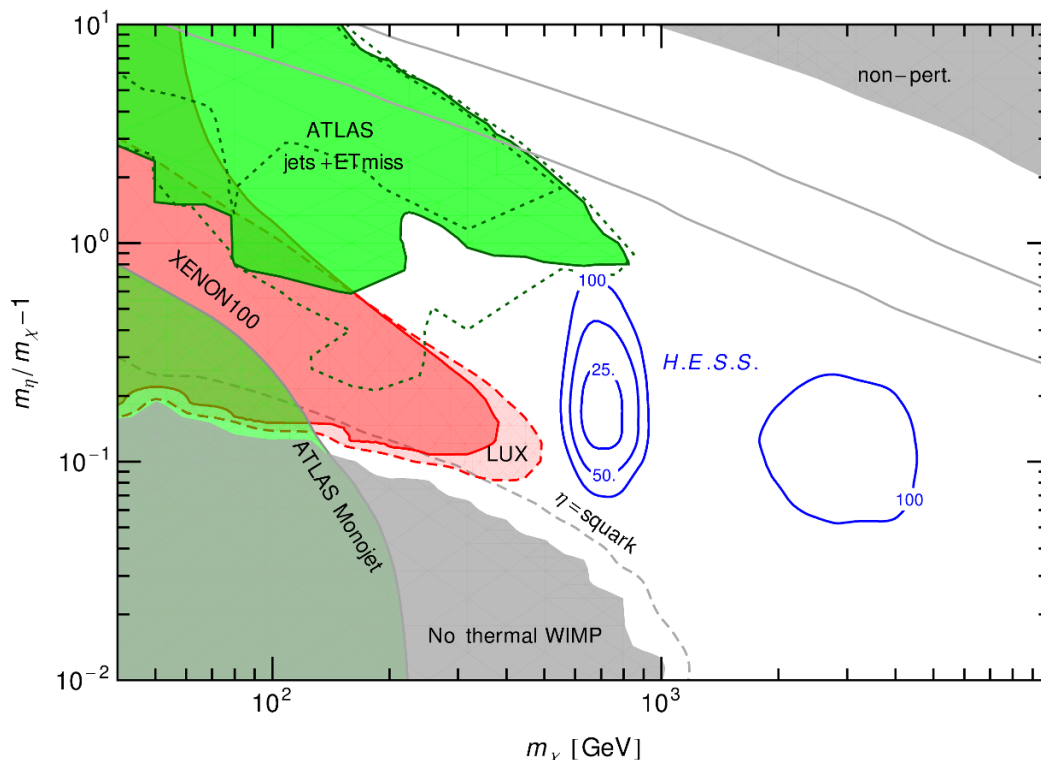


Figure 8. Constraints on thermally produced WIMP dark matter with a coloured mediator particle η . The green region is excluded at 95% C.L. by the ATLAS search [11] for jets and missing transverse energy. For comparison, the red shaded area is excluded by direct searches. The blue lines indicate the regions excluded by the search for an internal bremsstrahlung feature in the gamma-ray spectrum from the central galactic halo measured by H.E.S.S. [7], assuming a boost factor 25, 50 or 100, respectively [23]. Within the grey shaded region in the lower left corner, thermal production cannot make up for the whole dark matter abundance due to efficient coannihilations. Within the upper right corner, non-perturbatively large values of $f \gtrsim 10$ would be required. Below the upper(lower) gray line $\Gamma_\eta/m_\eta < 0.5(0.1)$. The gray dashed line indicates the masses for which the coupling of the mediator equals the one of a squark.

4.3 Exclusion for a thermal relic

By requiring that thermal freeze-out yields a relic abundance that coincides with the value measured by Planck [2], it is possible to fix the coupling $f = f_{\text{th}}(m_\eta, m_\chi)$ between dark matter χ , the mediator η and the SM quarks for each set of masses. Under this assumption, the model has only two free parameters, which we take to be the dark matter mass m_χ and the mass splitting $\delta = m_\eta/m_\chi - 1$. The collider limits considered here can be translated into an exclusion region, which we show in figure 8 (green region). For mass splitting $\delta = 1$, it reaches up to $m_\chi \sim 1$ TeV. However, for smaller or larger mass splitting, much lighter masses remain allowed. On the one hand, for much larger splitting, the mediator η becomes too heavy to be produced effectively. For much smaller splitting, on the other hand, two effects play a role: first, the collider search becomes less effective in this regime. Second, the coupling f_{th} gets very small due to efficient coannihilations. The combination of these effects also leads to the relatively large uncertainties in the exclusion region (green dotted

lines), in particular as the thermal cross section and the LHC exclusion happen to exhibit a fairly similar dependence on the mass splitting in certain regions of parameter space, see e.g. figure 4. For comparison, direct detection mostly probes a region with smaller mass splitting, due to the resonant enhancement of the nucleon scattering cross section for $\delta < 1$ (red regions; note that for LUX only limits on spin independent scattering are available at present). The limits from indirect detection are currently not sensitive to the flux expected for a thermal relic, if the standard Einasto profile from [23] is adopted. However, if the flux is enhanced by a boost factor of order 25–100, they probe the multi-TeV region (blue contour lines). For comparison, we also show a constraint inferred from mono-jet searches for nearly degenerate particle spectra [86], which is sensitive to very small splittings for low dark matter masses.

5 Conclusions

The Large Hadron Collider offers a unique environment to search for dark matter particles with masses below ~ 1 TeV through their possible production in partonic collisions. To optimize the search it is convenient to identify simplified models that characterize the signals of a larger class of dark matter models. In this paper we have focused on a model with Majorana dark matter particles that couple to the up-type quarks via one or several coloured mediators and which produces a signal consisting in two or more jets plus missing transverse energy, through the production and subsequent decay of the coloured scalar particles.

We have carefully analysed the production of coloured scalar particles at the LHC, considering not only the production via the strong gauge interaction, but also via the exchange of a dark matter particle in the t-channel. The latter production channel can be relevant and even dominant in some regions of the parameter space leading to the observed dark matter abundance via the thermal freeze-out of dark matter particles in the early Universe. More specifically, we have emphasized the importance of the partonic subprocess $uu \rightarrow \eta\eta$ mediated by a Majorana dark matter particle in the t-channel. Due to the enhancement of the rate by the square of the dark matter mass and due to the unsuppressed parton distribution function of up-quarks inside the proton, this process is the dominant production channel in large regions of the parameter space. Concretely, for large dark matter masses and a coloured scalar with comparable mass, we have found that the total production cross section of coloured scalars can be enhanced by more than two orders of magnitude compared to the production channels mediated by the strong interactions.

We have then derived limits on the parameters of the model employing the ATLAS search [11] for jets and missing transverse energy, based on $\mathcal{L} = 20.3 \text{ fb}^{-1}$ of data collected at a center of mass energy of 8 TeV. To re-interpret the analysis for the model considered here, we have computed the appropriate efficiencies for the relevant production channels, taking jet matching with two additional hard jets into account, for all signal regions containing two to four jets. Next, we have investigated the complementarity of the collider limits with those from direct detection and indirect detection experiments.

We have found that, for some regions of the parameter space of the model, the ATLAS searches imposes the strongest limits and rules out choices of parameters leading to the observed dark matter abundance via thermal production. For small mass splitting between the dark matter and the mediator, the collider limits are comparable to bounds from direct detection. However, if the mass splitting is of the same order as the dark matter mass, the ATLAS limits are considerably stronger than the latest bounds from XENON100 and LUX, reaching down to $\sigma_{\text{SI}} \sim 10^{-45} - 10^{-48} \text{cm}^2$ for $200 \text{ GeV} \lesssim m_\eta \lesssim 2 \text{ TeV}$ and $m_{\text{DM}} \lesssim m_\eta/2$. This is due to a relative suppression of the spin-independent scattering cross section for Majorana dark matter with chiral couplings, and the enhancement of the production at LHC described above.

Searches for sharp spectral features at gamma-ray telescopes are fully complementary in the multi-TeV region. However, for $m_{\text{DM}} \lesssim 1 \text{ TeV}$ direct detection and collider constraints in some cases even preclude the possibility of observing sharp spectral features at future gamma-ray telescopes for the standard choices of the astrophysical parameters. It is important to stress that these limits do not suffer from astrophysical uncertainties and are therefore very robust. We have estimated uncertainties arising from the determination of efficiencies and from higher-order contributions to the production cross section, which are typically $\lesssim \mathcal{O}(50)\%$ but can be larger in particular cases. Lastly, we have also considered an extension of the model by extra coloured scalars, inspired by the particle content of the Minimal Supersymmetric Standard Model. We have found that our main conclusions still remain for the scenarios in agreement with the flavour physics experiments.

Acknowledgments

We are grateful to Miguel Pato for earlier collaborations on which part of this work was based, and to Andreas Weiler for helpful discussions and for cross-checking efficiencies. This work has been partially supported by the DFG cluster of excellence “Origin and Structure of the Universe” and by the DFG Collaborative Research Center 676 “Particles, Strings and the Early Universe”. S.V. also acknowledges support from the DFG Graduiertenkolleg “Particle Physics at the Energy Frontier of New Phenomena”.

A Flavour constraints

The interaction term of the dark matter particle and the coloured scalars with the right-handed quarks in general violates the $\text{SU}(3)_{u_R}$ flavour symmetry. Therefore, it is necessary to check whether the stringent constraints arising from flavour physics are satisfied. In this appendix we discuss how two well-known possibilities to suppress flavour-changing neutral currents, namely degeneracy or alignment, can be realized within the toy-model considered in this work.

Consider first the possibility of a single coloured scalar η , but allowing for arbitrary couplings f_i to all right-handed quarks,

$$\mathcal{L} = -f_i \bar{u}_{Ri} \chi \eta \tag{A.1}$$

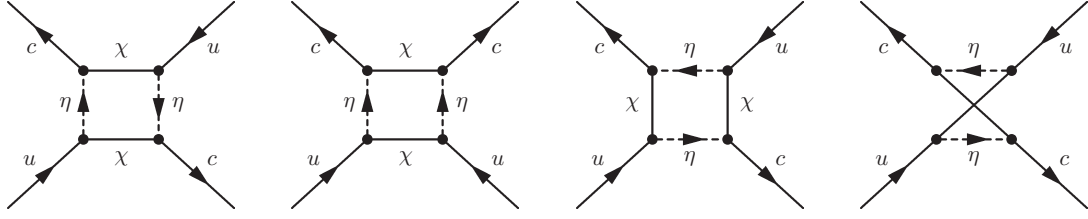


Figure 9. Box diagrams giving rise to a non-standard contribution to $D - \bar{D}$ mixing.

where $i = 1, 2, 3$ corresponds to u, c, t . In this case the box diagram shown in figure 9 gives a contribution to $D - \bar{D}$ mixing, which is strongly constrained by the measured value of the D -meson mass splitting Δm_D (note that there is no contribution to CP violation in presence of a single species η , such that constraints from ϵ_D do not apply). The box diagram gives a contribution to the operator

$$\mathcal{L} = \frac{\tilde{z}}{m_\eta^2} \bar{u}_R^\alpha \gamma^\mu c_R^\alpha \bar{u}_R^\beta \gamma_\mu c_R^\beta \quad (\text{A.2})$$

given by

$$\tilde{z} = -\frac{f_1^2 f_2^2}{96\pi^2} g_\chi (m_\chi^2/m_\eta^2) \quad (\text{A.3})$$

where $g_\chi(x) = 24x f_6(x) + 12\tilde{f}_6(x)$ (with $g_\chi(1) = 4/5$). The functions $f_6(x)$ and $\tilde{f}_6(x)$ are given e.g. in [87]. On the other hand, the experimental constraint inferred from measurements of Δm_D is $|\tilde{z}| \lesssim 5.7 \cdot 10^{-7} (m_\eta/\text{TeV})^2$ [87]. For $m_\eta \simeq m_\chi$, this translates into an upper bound

$$|f_2/f_1| \lesssim 0.026 \times (f_1)^{-2} \times \frac{m_\eta}{\text{TeV}}. \quad (\text{A.4})$$

Since thermal production requires typically $f_1 \sim \mathcal{O}(1)$, this means that η has to couple nearly exclusively to the up-quark, with very suppressed coupling to charm (or vice-versa). A possible exception are regions in parameter space with strong coannihilation for which $f_1 \ll 1$. For a generic $f_1 \sim \mathcal{O}(1)$, the flavour-vector f_i should be aligned with the mass eigenbasis of the quarks. This can be realized e.g. in the presence of a U(1) flavour symmetry under which $u_{R,L}$ and η transform with equal charge, while all other states are uncharged. This symmetry is then broken only by the CKM mixing in the left-handed quark sector, and thus this breaking should lead to a misalignment suppressed by the quark masses as well as CKM mixing angles. More precisely, one may consider a situation where $f_i \propto (1, 0, 0)$ at some high scale M . Due to renormalization group running, the quark mass matrices $M_u(\mu)$ and $M_d(\mu)$ are scale-dependent. This leads to a running of the diagonalization matrices $M_u^{\text{diag}}(\mu) = V_u^L(\mu) M_u(\mu) V_u^R(\mu)^\dagger$, with a similar expression for the down-type quarks. The left-handed rotations lead to the well-known running of the CKM matrix $V_{\text{CKM}}(\mu) = V_u^L(\mu) V_d^L(\mu)^\dagger$, while the right-handed rotations are unobservable in the Standard Model [88]. However, in the present case they lead to a flavour-dependent running of the dark matter couplings,

$$f_i(\mu) = V_u^R(\mu)_{ij} f_j(M), \quad (\text{A.5})$$

where we neglect flavour-insensitive contributions to the running and adopt a basis for which $V_u^R(M)_{ij} = \delta_{ij}$ (this is always possible by an appropriate flavor rotation in the right-handed up-type sector). Using the one-loop RGEs for the quark mass matrices from [89], one finds for the off-diagonal entry corresponding to $i = u$ and $j = c$

$$\frac{d}{d \ln \mu} V_u^R(\mu)_{uc}^\dagger = -\frac{3}{16\pi^2 v_{EW}^2} \frac{m_u m_c}{m_u^2 - m_c^2} (V_{ud} V_{cd}^* m_d^2 + V_{us} V_{cs}^* m_s^2 + V_{ub} V_{cb}^* m_b^2) \quad (\text{A.6})$$

where V_{ud} etc. denotes the CKM matrix elements. Thus, even for perfect alignment $f_i(M) = (f_1, 0, 0)$ at the high scale, the coupling to the second generation induced by the running is approximately

$$|f_2/f_1| \simeq |V_u^R(\mu)_{uc}| \sim \frac{3}{16\pi^2} \frac{m_u}{m_c} \frac{|V_{us} V_{cs}^* m_s^2 + V_{ub} V_{cb}^* m_b^2|}{v_{EW}^2} \ln \frac{M}{\mu} \sim 10^{-10} \quad (\text{A.7})$$

which is safely below the upper bound required from $D - \bar{D}$ mixing.

Alternatively, one may consider a situation where three additional scalars η_i are introduced, which are taken to transform under the $SU(3)_{uR}$ flavour symmetry. Then the allowed coupling is of the form

$$\mathcal{L} = -f \sum_i \bar{u}_{Ri} \chi \eta_i \quad (\text{A.8})$$

and the η_i are all mass-degenerate. One may consider a breaking of the symmetry in the scalar mass matrix, which induces non-degenerate mass eigenvalues of the η_i , and singles out a preferred basis, namely the mass eigenbasis (similar to the right-handed squarks in the MSSM). After rotating into this basis (as well as the mass basis for the quarks) the interaction term has the generic form

$$\mathcal{L} = -f K_{ij} \sum_i \bar{u}_{Ri} \chi \eta_j \quad (\text{A.9})$$

where K is a unitary matrix, which can have large off-diagonal entries. The resulting contribution to the box diagram will be proportional to [49]

$$\sum_{\alpha, \beta} K_{1\alpha} K_{2\alpha}^* K_{1\beta} K_{2\beta}^* F(m_{\eta_\alpha}, m_{\eta_\beta}) \quad (\text{A.10})$$

where F is a function of the masses. In the limit of degenerate masses this expression goes to zero by virtue of the unitarity condition $(KK^\dagger)_{12} = 0$. Lets assume for concreteness that the mixing with the third generation is negligible, similar as in the CKM matrix. In this case the box diagram gives a contribution

$$\tilde{z} = -\frac{f^4}{384\pi^2} g_\chi (m_\chi^2/m_\eta^2) \times \delta^2 \quad (\text{A.11})$$

with $\delta = K_{21} K_{11} (m_{\eta_1}^2 - m_{\eta_2}^2)/m_\eta^2$ and $m_\eta = (m_{\eta_1} + m_{\eta_2})/2$. Thus, the strong requirement of precise alignment $f_2/f_1 = K_{21}/K_{11}$ found above can be considerably relaxed provided the masses are quasi-degenerate. For order one mixing, the upper bound on \tilde{z} required from $D - \bar{D}$ mixing then translates into an upper bound on the mass splitting

$$\frac{|m_{\eta_1} - m_{\eta_2}|}{m_{\eta_1} + m_{\eta_2}} \lesssim 0.026 \times (f_1)^{-2} \times \frac{m_\eta}{\text{TeV}}. \quad (\text{A.12})$$

Thus, in both cases discussed above, the flavour constraints can be fulfilled in presence of an (approximate) flavour symmetry.

Open Access. This article is distributed under the terms of the Creative Commons Attribution License ([CC-BY 4.0](https://creativecommons.org/licenses/by/4.0/)), which permits any use, distribution and reproduction in any medium, provided the original author(s) and source are credited.

References

- [1] G. Bertone, D. Hooper and J. Silk, *Particle dark matter: Evidence, candidates and constraints*, *Phys. Rept.* **405** (2005) 279 [[hep-ph/0404175](https://arxiv.org/abs/hep-ph/0404175)] [[INSPIRE](#)].
- [2] PLANCK collaboration, P.A.R. Ade et al., *Planck 2013 results. XVI. Cosmological parameters*, [arXiv:1303.5076](https://arxiv.org/abs/1303.5076) [[INSPIRE](#)].
- [3] XENON100 collaboration, E. Aprile et al., *Dark Matter Results from 225 Live Days of XENON100 Data*, *Phys. Rev. Lett.* **109** (2012) 181301 [[arXiv:1207.5988](https://arxiv.org/abs/1207.5988)] [[INSPIRE](#)].
- [4] LUX collaboration, D.S. Akerib et al., *First results from the LUX dark matter experiment at the Sanford Underground Research Facility*, *Phys. Rev. Lett.* **112** (2014) 091303 [[arXiv:1310.8214](https://arxiv.org/abs/1310.8214)] [[INSPIRE](#)].
- [5] FERMI-LAT collaboration, M. Ackermann et al., *Search for Gamma-ray Spectral Lines with the Fermi Large Area Telescope and Dark Matter Implications*, *Phys. Rev. D* **88** (2013) 082002 [[arXiv:1305.5597](https://arxiv.org/abs/1305.5597)] [[INSPIRE](#)].
- [6] AMS collaboration, M. Aguilar et al., *First Result from the Alpha Magnetic Spectrometer on the International Space Station: Precision Measurement of the Positron Fraction in Primary Cosmic Rays of 0.5–350 GeV*, *Phys. Rev. Lett.* **110** (2013) 141102 [[INSPIRE](#)].
- [7] H.E.S.S. collaboration, A. Abramowski et al., *Search for photon line-like signatures from Dark Matter annihilations with H.E.S.S.*, *Phys. Rev. Lett.* **110** (2013) 041301 [[arXiv:1301.1173](https://arxiv.org/abs/1301.1173)] [[INSPIRE](#)].
- [8] J. Aleksic et al., *Optimized dark matter searches in deep observations of Segue 1 with MAGIC*, *JCAP* **02** (2014) 008 [[arXiv:1312.1535](https://arxiv.org/abs/1312.1535)] [[INSPIRE](#)].
- [9] ICECUBE collaboration, M.G. Aartsen et al., *Search for dark matter annihilations in the Sun with the 79-string IceCube detector*, *Phys. Rev. Lett.* **110** (2013) 131302 [[arXiv:1212.4097](https://arxiv.org/abs/1212.4097)] [[INSPIRE](#)].
- [10] CMS collaboration, *Search for supersymmetry in final states with missing transverse energy and 0, 1, 2, 3, or at least 4 b-quark jets in 8 TeV pp collisions using the variable AlphaT*, [CMS-PAS-SUS-12-028](#).
- [11] ATLAS collaboration, *Search for squarks and gluinos with the ATLAS detector in final states with jets and missing transverse momentum and 20.3 fb⁻¹ of $\sqrt{s} = 8$ TeV proton-proton collision data*, [ATLAS-CONF-2013-047](#) [ATLAS-COM-CONF-2013-049].
- [12] CMS collaboration, *Search for dark matter and large extra dimensions in monojet events in pp collisions at $\sqrt{s} = 7$ TeV*, *JHEP* **09** (2012) 094 [[arXiv:1206.5663](https://arxiv.org/abs/1206.5663)] [[INSPIRE](#)].
- [13] ATLAS collaboration, *Search for New Phenomena in Monojet plus Missing Transverse Momentum Final States using 10 fb⁻¹ of pp Collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector at the LHC*, [ATLAS-CONF-2012-147](#) [ATLAS-COM-CONF-2012-190].
- [14] XENON1T collaboration, E. Aprile, *The XENON1T Dark Matter Search Experiment*, [arXiv:1206.6288](https://arxiv.org/abs/1206.6288) [[INSPIRE](#)].
- [15] D.C. Malling et al., *After LUX: The LZ Program*, [arXiv:1110.0103](https://arxiv.org/abs/1110.0103) [[INSPIRE](#)].

- [16] K. Bernlöhner et al., *Monte Carlo design studies for the Cherenkov Telescope Array*, *Astropart. Phys.* **43** (2013) 171 [[arXiv:1210.3503](#)] [[INSPIRE](#)].
- [17] J. Hisano, K. Ishiwata and N. Nagata, *Direct Detection of Dark Matter Degenerate with Colored Particles in Mass*, *Phys. Lett. B* **706** (2011) 208 [[arXiv:1110.3719](#)] [[INSPIRE](#)].
- [18] M. Garny, A. Ibarra, M. Pato and S. Vogl, *Closing in on mass-degenerate dark matter scenarios with antiprotons and direct detection*, *JCAP* **11** (2012) 017 [[arXiv:1207.1431](#)] [[INSPIRE](#)].
- [19] K. Hamaguchi, S.P. Liew, T. Moroi and Y. Yamamoto, *Isospin-Violating Dark Matter with Colored Mediators*, *JHEP* **05** (2014) 086 [[arXiv:1403.0324](#)] [[INSPIRE](#)].
- [20] M. Garny, A. Ibarra and S. Vogl, *Dark matter annihilations into two light fermions and one gauge boson: General analysis and antiproton constraints*, *JCAP* **04** (2012) 033 [[arXiv:1112.5155](#)] [[INSPIRE](#)].
- [21] M. Asano, T. Bringmann and C. Weniger, *Indirect dark matter searches as a probe of degenerate particle spectra*, *Phys. Lett. B* **709** (2012) 128 [[arXiv:1112.5158](#)] [[INSPIRE](#)].
- [22] T. Bringmann, X. Huang, A. Ibarra, S. Vogl and C. Weniger, *Fermi LAT Search for Internal Bremsstrahlung Signatures from Dark Matter Annihilation*, *JCAP* **07** (2012) 054 [[arXiv:1203.1312](#)] [[INSPIRE](#)].
- [23] M. Garny, A. Ibarra, M. Pato and S. Vogl, *Internal bremsstrahlung signatures in light of direct dark matter searches*, *JCAP* **12** (2013) 046 [[arXiv:1306.6342](#)] [[INSPIRE](#)].
- [24] A. Ibarra, M. Totzauer and S. Wild, *High-energy neutrino signals from the Sun in dark matter scenarios with internal bremsstrahlung*, *JCAP* **12** (2013) 043 [[arXiv:1311.1418](#)] [[INSPIRE](#)].
- [25] A. Ibarra, M. Totzauer and S. Wild, *Higher order dark matter annihilations in the Sun and implications for IceCube*, *JCAP* **04** (2014) 012 [[arXiv:1402.4375](#)] [[INSPIRE](#)].
- [26] S. Chang, R. Edezhath, J. Hutchinson and M. Luty, *Effective WIMPs*, *Phys. Rev. D* **89** (2014) 015011 [[arXiv:1307.8120](#)] [[INSPIRE](#)].
- [27] H. An, L.-T. Wang and H. Zhang, *Dark matter with t -channel mediator: a simple step beyond contact interaction*, [[arXiv:1308.0592](#)] [[INSPIRE](#)].
- [28] Y. Bai and J. Berger, *Fermion Portal Dark Matter*, *JHEP* **11** (2013) 171 [[arXiv:1308.0612](#)] [[INSPIRE](#)].
- [29] A. DiFranzo, K.I. Nagao, A. Rajaraman and T.M.P. Tait, *Simplified Models for Dark Matter Interacting with Quarks*, *JHEP* **11** (2013) 014 [[arXiv:1308.2679](#)] [[INSPIRE](#)].
- [30] J.N. Ng and A. de la Puente, *Top Quark as a Dark Portal and Neutrino Mass Generation*, *Phys. Lett. B* **727** (2013) 204 [[arXiv:1307.2606](#)] [[INSPIRE](#)].
- [31] L. Bergstrom, *Radiative Processes in Dark Matter Photino Annihilation*, *Phys. Lett. B* **225** (1989) 372 [[INSPIRE](#)].
- [32] T. Bringmann, L. Bergstrom and J. Edsjo, *New Gamma-Ray Contributions to Supersymmetric Dark Matter Annihilation*, *JHEP* **01** (2008) 049 [[arXiv:0710.3169](#)] [[INSPIRE](#)].
- [33] T. Bringmann, F. Calore, G. Vertongen and C. Weniger, *On the Relevance of Sharp Gamma-Ray Features for Indirect Dark Matter Searches*, *Phys. Rev. D* **84** (2011) 103525 [[arXiv:1106.1874](#)] [[INSPIRE](#)].

- [34] M. Beltrán, D. Hooper, E.W. Kolb and Z.C. Krusberg, *Deducing the nature of dark matter from direct and indirect detection experiments in the absence of collider signatures of new physics*, *Phys. Rev. D* **80** (2009) 043509 [[arXiv:0808.3384](#)] [[INSPIRE](#)].
- [35] M. Beltrán, D. Hooper, E.W. Kolb, Z.A.C. Krusberg and T.M.P. Tait, *Maverick dark matter at colliders*, *JHEP* **09** (2010) 037 [[arXiv:1002.4137](#)] [[INSPIRE](#)].
- [36] A. Rajaraman, W. Shepherd, T.M.P. Tait and A.M. Wijangco, *LHC Bounds on Interactions of Dark Matter*, *Phys. Rev. D* **84** (2011) 095013 [[arXiv:1108.1196](#)] [[INSPIRE](#)].
- [37] P.J. Fox, R. Harnik, J. Kopp and Y. Tsai, *Missing Energy Signatures of Dark Matter at the LHC*, *Phys. Rev. D* **85** (2012) 056011 [[arXiv:1109.4398](#)] [[INSPIRE](#)].
- [38] G. Busoni, A. De Simone, E. Morgante and A. Riotto, *On the Validity of the Effective Field Theory for Dark Matter Searches at the LHC*, *Phys. Lett. B* **728** (2014) 412 [[arXiv:1307.2253](#)] [[INSPIRE](#)].
- [39] O. Buchmueller, M.J. Dolan and C. McCabe, *Beyond Effective Field Theory for Dark Matter Searches at the LHC*, *JHEP* **01** (2014) 025 [[arXiv:1308.6799](#)] [[INSPIRE](#)].
- [40] P. Ciafaloni et al., *On the Importance of Electroweak Corrections for Majorana Dark Matter Indirect Detection*, *JCAP* **06** (2011) 018 [[arXiv:1104.2996](#)] [[INSPIRE](#)].
- [41] N.F. Bell et al., *W/Z Bremsstrahlung as the Dominant Annihilation Channel for Dark Matter, Revisited*, *Phys. Lett. B* **706** (2011) 6 [[arXiv:1104.3823](#)] [[INSPIRE](#)].
- [42] M. Garny, A. Ibarra and S. Vogl, *Antiproton constraints on dark matter annihilations from internal electroweak bremsstrahlung*, *JCAP* **07** (2011) 028 [[arXiv:1105.5367](#)] [[INSPIRE](#)].
- [43] J. Kopp, L. Michaels and J. Smirnov, *Loopy Constraints on Leptophilic Dark Matter and Internal Bremsstrahlung*, *JCAP* **04** (2014) 022 [[arXiv:1401.6457](#)] [[INSPIRE](#)].
- [44] S. Chang, R. Edezhath, J. Hutchinson and M. Luty, *Leptophilic Effective WIMPs*, [arXiv:1402.7358](#) [[INSPIRE](#)].
- [45] Y. Bai and J. Berger, *Lepton Portal Dark Matter*, [arXiv:1402.6696](#) [[INSPIRE](#)].
- [46] CMS collaboration, *Search for supersymmetry in hadronic final states with missing transverse energy using the variables α_T and b-quark multiplicity in pp collisions at $\sqrt{s} = 8$ TeV*, *Eur. Phys. J. C* **73** (2013) 2568 [[arXiv:1303.2985](#)] [[INSPIRE](#)].
- [47] CMS collaboration, *Search for New Physics in the Multijets and Missing Momentum Final State in Proton-Proton Collisions at 8 TeV*, CMS-PAS-SUS-13-012 [[arXiv:1402.4770](#)].
- [48] M. Papucci, A. Vichi and K.M. Zurek, *Monojet versus rest of the world I: t-channel Models*, [arXiv:1402.2285](#) [[INSPIRE](#)].
- [49] Y. Nir and N. Seiberg, *Should squarks be degenerate?*, *Phys. Lett. B* **309** (1993) 337 [[hep-ph/9304307](#)] [[INSPIRE](#)].
- [50] G. D'Ambrosio, G.F. Giudice, G. Isidori and A. Strumia, *Minimal flavor violation: An effective field theory approach*, *Nucl. Phys. B* **645** (2002) 155 [[hep-ph/0207036](#)] [[INSPIRE](#)].
- [51] K. Blum, Y. Grossman, Y. Nir and G. Perez, *Combining K^0 - \bar{K}^0 mixing and D^0 - \bar{D}^0 mixing to constrain the flavor structure of new physics*, *Phys. Rev. Lett.* **102** (2009) 211802 [[arXiv:0903.2118](#)] [[INSPIRE](#)].
- [52] K. Griest and D. Seckel, *Three exceptions in the calculation of relic abundances*, *Phys. Rev. D* **43** (1991) 3191 [[INSPIRE](#)].

- [53] G. Bélanger et al., *Indirect search for dark matter with MicrOMEGAs2.4*, *Comput. Phys. Commun.* **182** (2011) 842 [[arXiv:1004.1092](#)] [[INSPIRE](#)].
- [54] A. De Simone, G.F. Giudice and A. Strumia, *Benchmarks for Dark Matter Searches at the LHC*, [arXiv:1402.6287](#) [[INSPIRE](#)].
- [55] J.R. Ellis, T. Falk and K.A. Olive, *Neutralino-stau coannihilation and the cosmological upper limit on the mass of the lightest supersymmetric particle*, *Phys. Lett.* **B 444** (1998) 367 [[hep-ph/9810360](#)] [[INSPIRE](#)].
- [56] L. Bergstrom and P. Ullio, *Full one loop calculation of neutralino annihilation into two photons*, *Nucl. Phys.* **B 504** (1997) 27 [[hep-ph/9706232](#)] [[INSPIRE](#)].
- [57] Z. Bern, P. Gondolo and M. Perelstein, *Neutralino annihilation into two photons*, *Phys. Lett.* **B 411** (1997) 86 [[hep-ph/9706538](#)] [[INSPIRE](#)].
- [58] P. Ullio and L. Bergstrom, *Neutralino annihilation into a photon and a Z boson*, *Phys. Rev.* **D 57** (1998) 1962 [[hep-ph/9707333](#)] [[INSPIRE](#)].
- [59] L. Bergstrom, T. Bringmann, M. Eriksson and M. Gustafsson, *Gamma rays from Kaluza-Klein dark matter*, *Phys. Rev. Lett.* **94** (2005) 131301 [[astro-ph/0410359](#)] [[INSPIRE](#)].
- [60] L. Bergstrom, T. Bringmann, M. Eriksson and M. Gustafsson, *Gamma rays from heavy neutralino dark matter*, *Phys. Rev. Lett.* **95** (2005) 241301 [[hep-ph/0507229](#)] [[INSPIRE](#)].
- [61] R. Flores, K.A. Olive and S. Rudaz, *Radiative Processes in Lsp Annihilation*, *Phys. Lett.* **B 232** (1989) 377 [[INSPIRE](#)].
- [62] M. Drees, G. Jungman, M. Kamionkowski and M.M. Nojiri, *Neutralino annihilation into gluons*, *Phys. Rev.* **D 49** (1994) 636 [[hep-ph/9306325](#)] [[INSPIRE](#)].
- [63] N.F. Bell, J.B. Dent, T.D. Jacques and T.J. Weiler, *Dark Matter Annihilation Signatures from Electroweak Bremsstrahlung*, *Phys. Rev.* **D 84** (2011) 103517 [[arXiv:1101.3357](#)] [[INSPIRE](#)].
- [64] N.F. Bell, A.J. Brennan and T.D. Jacques, *Neutrino signals from electroweak bremsstrahlung in solar WIMP annihilation*, *JCAP* **10** (2012) 045 [[arXiv:1206.2977](#)] [[INSPIRE](#)].
- [65] P. Ciafaloni et al., *Initial State Radiation in Majorana Dark Matter Annihilations*, *JCAP* **10** (2011) 034 [[arXiv:1107.4453](#)] [[INSPIRE](#)].
- [66] P. Ciafaloni, D. Comelli, A. De Simone, A. Riotto and A. Urbano, *Electroweak Bremsstrahlung for Wino-Like Dark Matter Annihilations*, *JCAP* **06** (2012) 016 [[arXiv:1202.0692](#)] [[INSPIRE](#)].
- [67] A. De Simone, A. Monin, A. Thamm and A. Urbano, *On the effective operators for Dark Matter annihilations*, *JCAP* **02** (2013) 039 [[arXiv:1301.1486](#)] [[INSPIRE](#)].
- [68] K. Fukushima, Y. Gao, J. Kumar and D. Marfatia, *Bremsstrahlung signatures of dark matter annihilation in the Sun*, *Phys. Rev.* **D 86** (2012) 076014 [[arXiv:1208.1010](#)] [[INSPIRE](#)].
- [69] F. Luo and T. You, *Enhancement of Majorana Dark Matter Annihilation Through Higgs Bremsstrahlung*, *JCAP* **12** (2013) 024 [[arXiv:1310.5129](#)] [[INSPIRE](#)].
- [70] G. Jungman, M. Kamionkowski and K. Griest, *Supersymmetric dark matter*, *Phys. Rept.* **267** (1996) 195 [[hep-ph/9506380](#)] [[INSPIRE](#)].
- [71] M. Drees and M. Nojiri, *Neutralino-nucleon scattering revisited*, *Phys. Rev.* **D 48** (1993) 3483 [[hep-ph/9307208](#)] [[INSPIRE](#)].

- [72] M. Garny, A. Ibarra, M. Pato and S. Vogl, *On the spin-dependent sensitivity of XENON100*, *Phys. Rev. D* **87** (2013) 056002 [[arXiv:1211.4573](#)] [[INSPIRE](#)].
- [73] P. Gondolo and S. Scopel, *On the sbottom resonance in dark matter scattering*, *JCAP* **10** (2013) 032 [[arXiv:1307.4481](#)] [[INSPIRE](#)].
- [74] M. Felizardo et al., *Final Analysis and Results of the Phase II SIMPLE Dark Matter Search*, *Phys. Rev. Lett.* **108** (2012) 201302 [[arXiv:1106.3014](#)] [[INSPIRE](#)].
- [75] COUPP collaboration, E. Behnke et al., *First Dark Matter Search Results from a 4-kg CF₃I Bubble Chamber Operated in a Deep Underground Site*, *Phys. Rev. D* **86** (2012) 052001 [[arXiv:1204.3094](#)] [[INSPIRE](#)].
- [76] R. Mahbubani, M. Papucci, G. Perez, J.T. Ruderman and A. Weiler, *Light Nondegenerate Squarks at the LHC*, *Phys. Rev. Lett.* **110** (2013) 151804 [[arXiv:1212.3328](#)] [[INSPIRE](#)].
- [77] M. Krämer et al., *Supersymmetry production cross sections in pp collisions at $\sqrt{s} = 7$ TeV*, [arXiv:1206.2892](#) [[INSPIRE](#)].
- [78] LHC SUSY Cross section Working Group, [https://twiki.cern.ch/twiki/bin/view/LHCPhysics/SUSYCross sections](https://twiki.cern.ch/twiki/bin/view/LHCPhysics/SUSYCross%20sections).
- [79] W. Hollik, J.M. Lindert and D. Pagani, *NLO corrections to squark-squark production and decay at the LHC*, *JHEP* **03** (2013) 139 [[arXiv:1207.1071](#)] [[INSPIRE](#)].
- [80] A. Pukhov, *CalcHEP 2.3: MSSM, structure functions, event generation, batchs and generation of matrix elements for other packages*, [hep-ph/0412191](#) [[INSPIRE](#)].
- [81] J. Pumplin et al., *New generation of parton distributions with uncertainties from global QCD analysis*, *JHEP* **07** (2002) 012 [[hep-ph/0201195](#)] [[INSPIRE](#)].
- [82] J. Alwall, M. Herquet, F. Maltoni, O. Mattelaer and T. Stelzer, *MadGraph 5: Going Beyond*, *JHEP* **06** (2011) 128 [[arXiv:1106.0522](#)] [[INSPIRE](#)].
- [83] DELPHES 3 collaboration, J. de Favereau et al., *DELPHES 3, A modular framework for fast simulation of a generic collider experiment*, *JHEP* **02** (2014) 057 [[arXiv:1307.6346](#)] [[INSPIRE](#)].
- [84] T. Sjöstrand, S. Mrenna and P.Z. Skands, *A Brief Introduction to PYTHIA 8.1*, *Comput. Phys. Commun.* **178** (2008) 852 [[arXiv:0710.3820](#)] [[INSPIRE](#)].
- [85] XENON100 collaboration, E. Aprile et al., *Limits on spin-dependent WIMP-nucleon cross sections from 225 live days of XENON100 data*, *Phys. Rev. Lett.* **111** (2013) 021301 [[arXiv:1301.6620](#)] [[INSPIRE](#)].
- [86] H.K. Dreiner, M. Krämer and J. Tattersall, *How low can SUSY go? Matching, monojets and compressed spectra*, *Europhys. Lett.* **99** (2012) 61001 [[arXiv:1207.1613](#)] [[INSPIRE](#)].
- [87] O. Gedalia, Y. Grossman, Y. Nir and G. Perez, *Lessons from Recent Measurements of D^0 - \bar{D}^0 Mixing*, *Phys. Rev. D* **80** (2009) 055024 [[arXiv:0906.1879](#)] [[INSPIRE](#)].
- [88] E. Ma and S. Pakvasa, *Variation of Mixing Angles and Masses With q^2 in the Standard Six Quark Model*, *Phys. Rev. D* **20** (1979) 2899 [[INSPIRE](#)].
- [89] V.D. Barger, M.S. Berger and P. Ohmann, *Universal evolution of CKM matrix elements*, *Phys. Rev. D* **47** (1993) 2038 [[hep-ph/9210260](#)] [[INSPIRE](#)].