



Interpretable Machine Learning for Ionosphere Forecasting with Uncertainty Quantification

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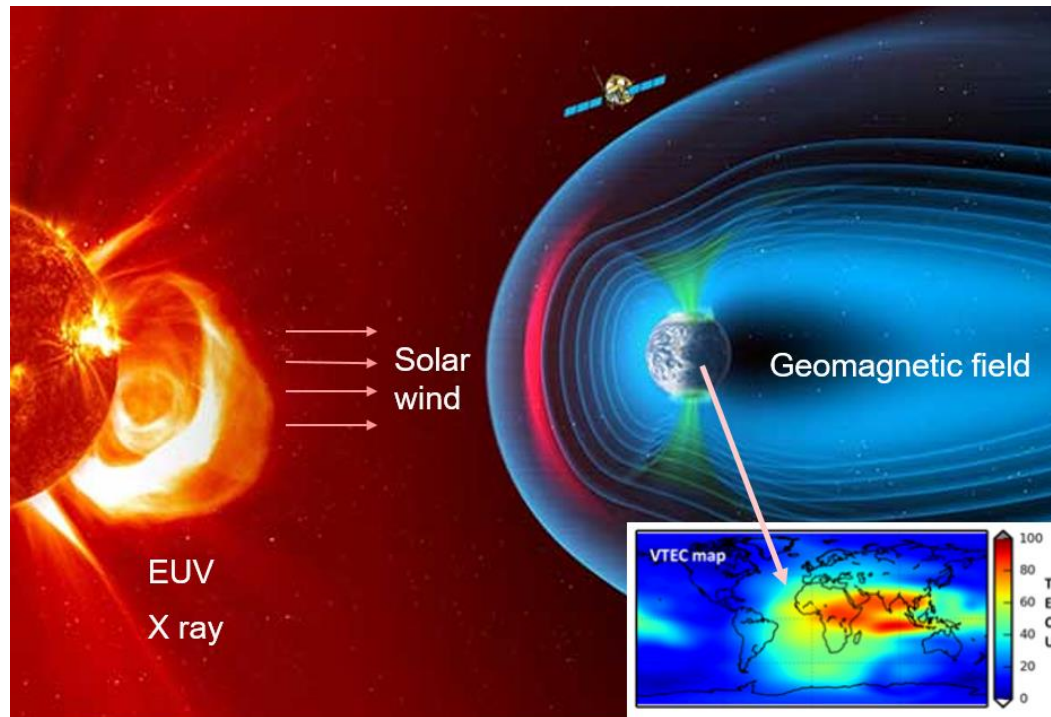
1st Workshop on Data Science for GNSS Remote Sensing (D4G), GFZ Potsdam

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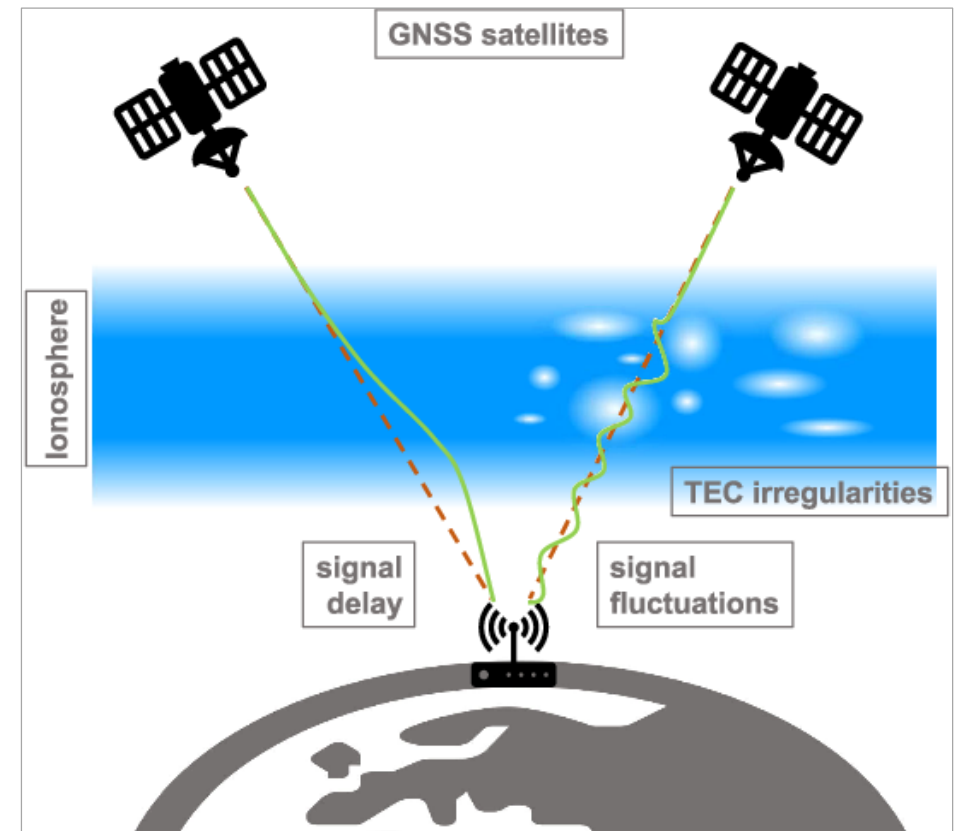
Research problem

- Ionospheric refraction of GNSS signals
- Dual-frequency obs. → integrated electron density
- Vertical Total Electron Content (VTEC)



Ionospheric VTEC map

Image source: ESA (background), DGFI-TUM (VTEC map).



Source: <https://www.semanticscholar.org/paper/Detection-of-GNSS-Ionospheric-Scintillations-Based-Linty-Farasin/3bc53da7342d4cdcd1a8bacfdc92651aeb62d5dc>

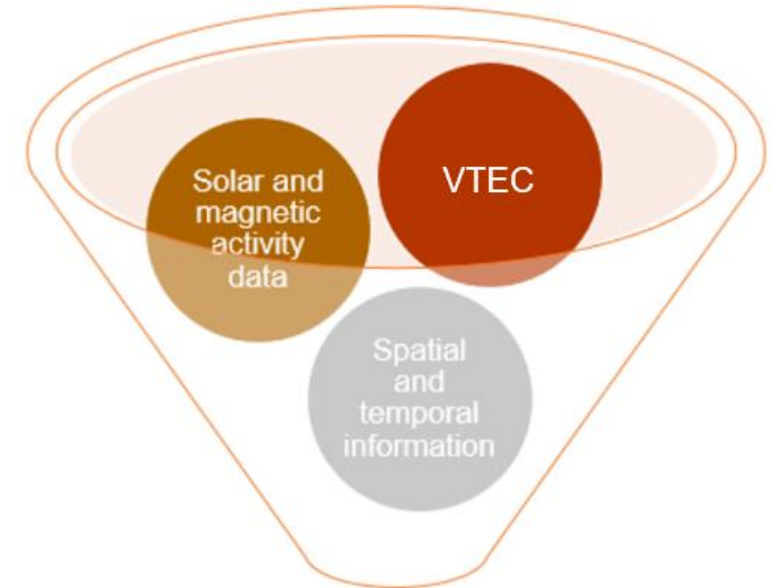
Research problem

Objectives:

- Model / forecast VTEC accurately and precisely
 - Including solar-terrestrial processes (space weather)

- Nonlinear processes
- Complex, dynamical conditions
- Limited understanding
- Unkown function

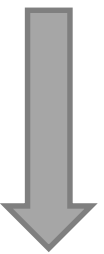
- How to find a function?



Research problem

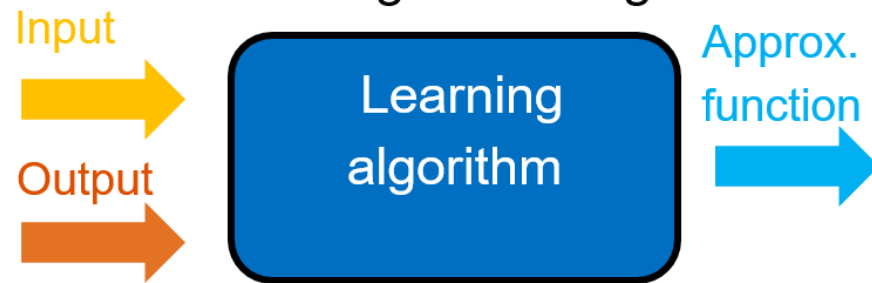
I. How to find a function?

- “Learn” from the (high-dimensional) data
- Approximate nonlinear functions

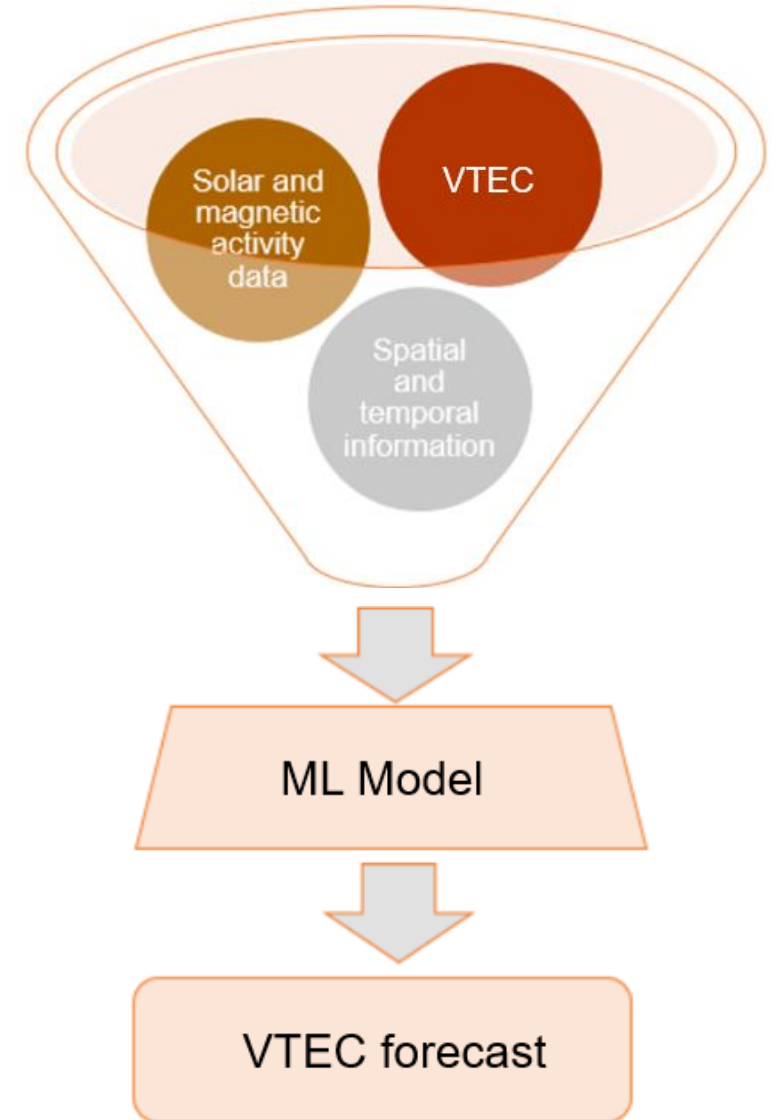
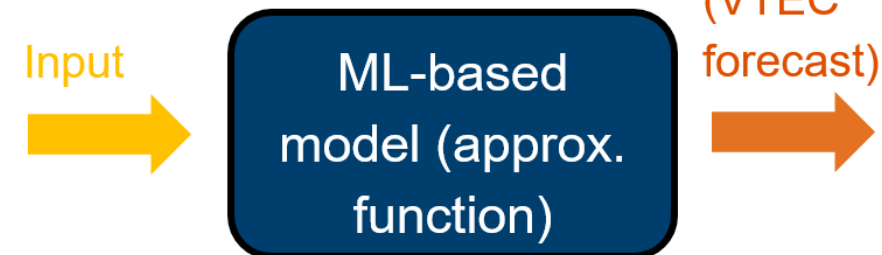

 Machine Learning (ML)

Supervised learning

Training / Learning:



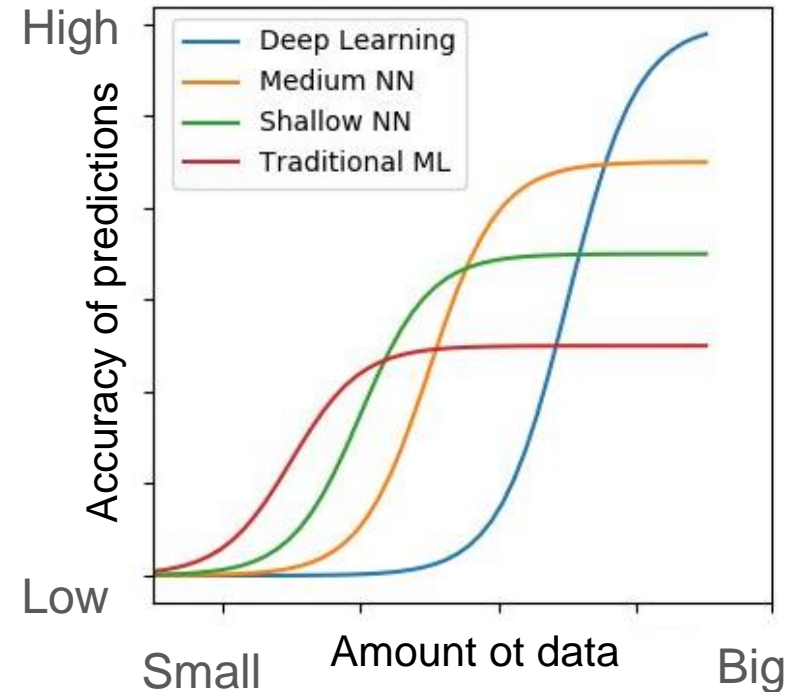
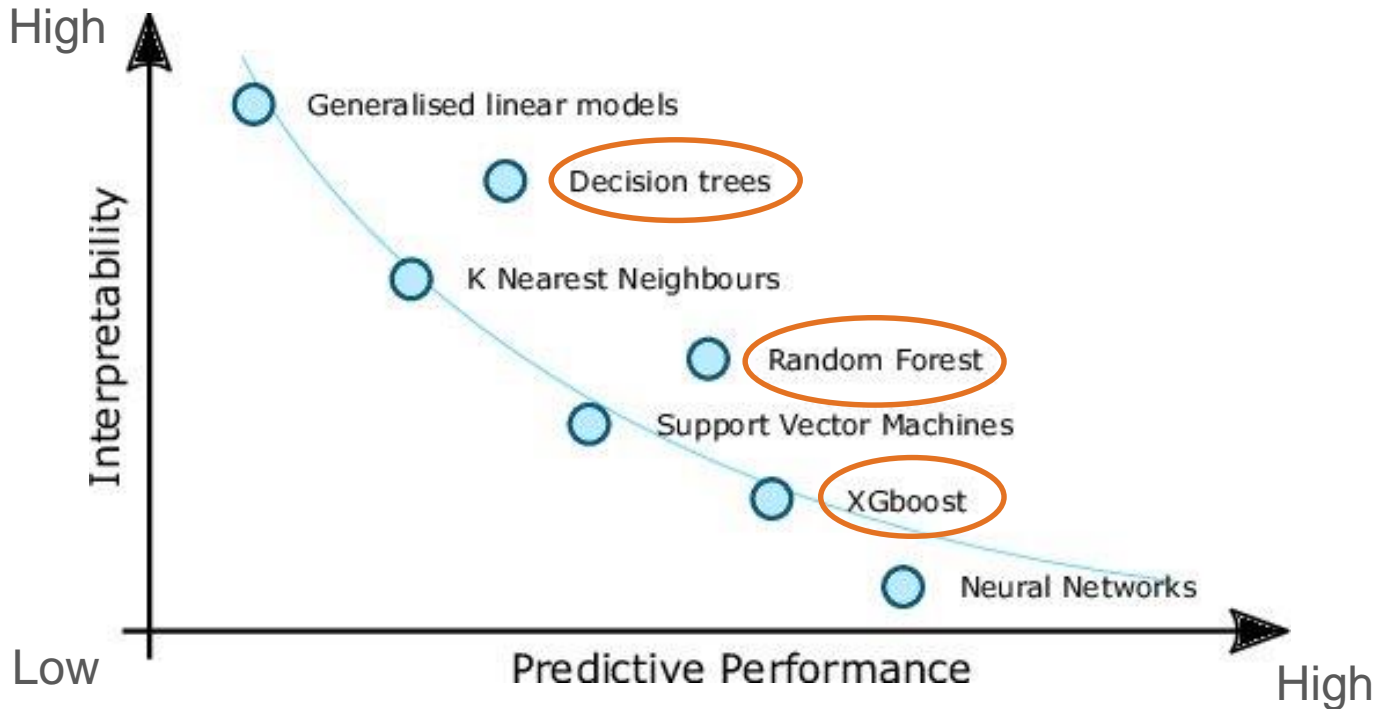
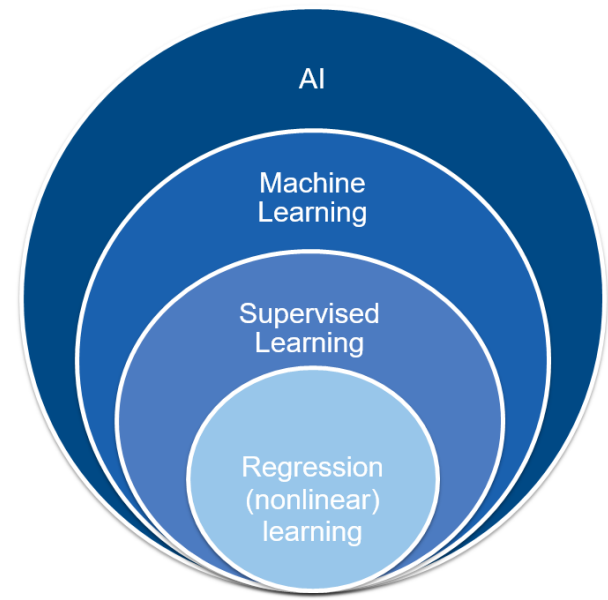
Model Prediction:



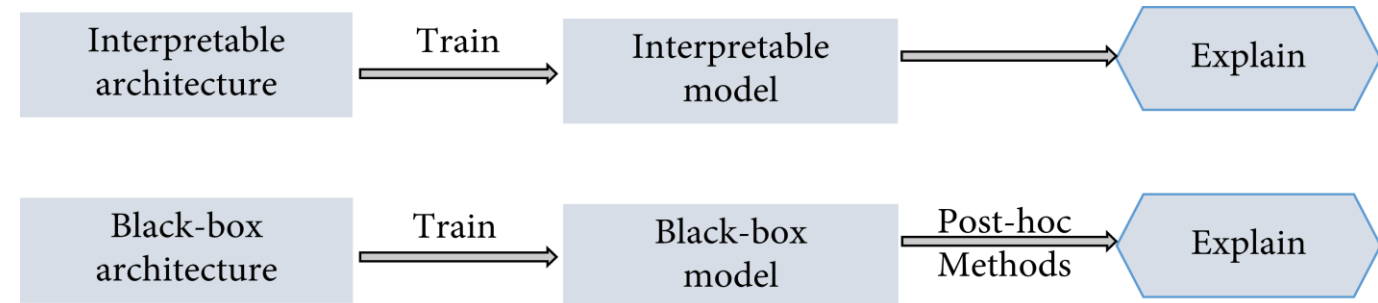
Learning algorithms

I. How to find a function?

- Linear models → (Deep) Neural networks
- Low complexity → High complexity
- Interpretability / performance trade-off



- Aim → Predictions:
 - Accurate and precise
 - Reliable
 - Trustworthy
 - Explainable / Interpretable



Source: <https://doi.org/10.1155/2021/2939334>



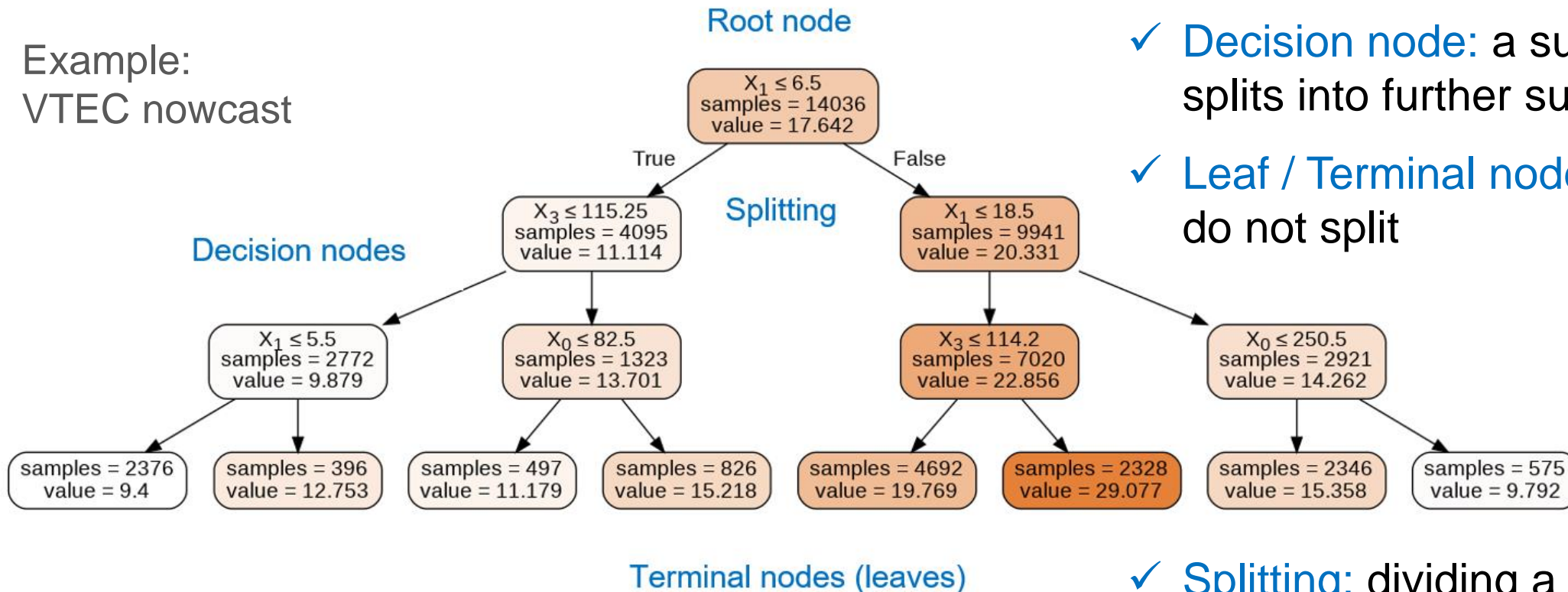
II. How to accomplish that?

- ✓ (Permutation) feature importance
- ✓ Feature interaction
- ✓ Partial dependence
- ✓ LIME (local surrogate)
- ✓ SHAP (SHapley Additive exPlanations)
-

1. Using interpretable models

Decision tree learning

Example:
VTEC nowcast



✓ **Root node:** entire dataset; further divided into 2 subnodes

✓ **Decision node:** a subnode that splits into further subnodes

✓ **Leaf / Terminal node:** nodes that do not split

✓ **Splitting:** dividing a node into 2 subnodes by calculating reduction in variance

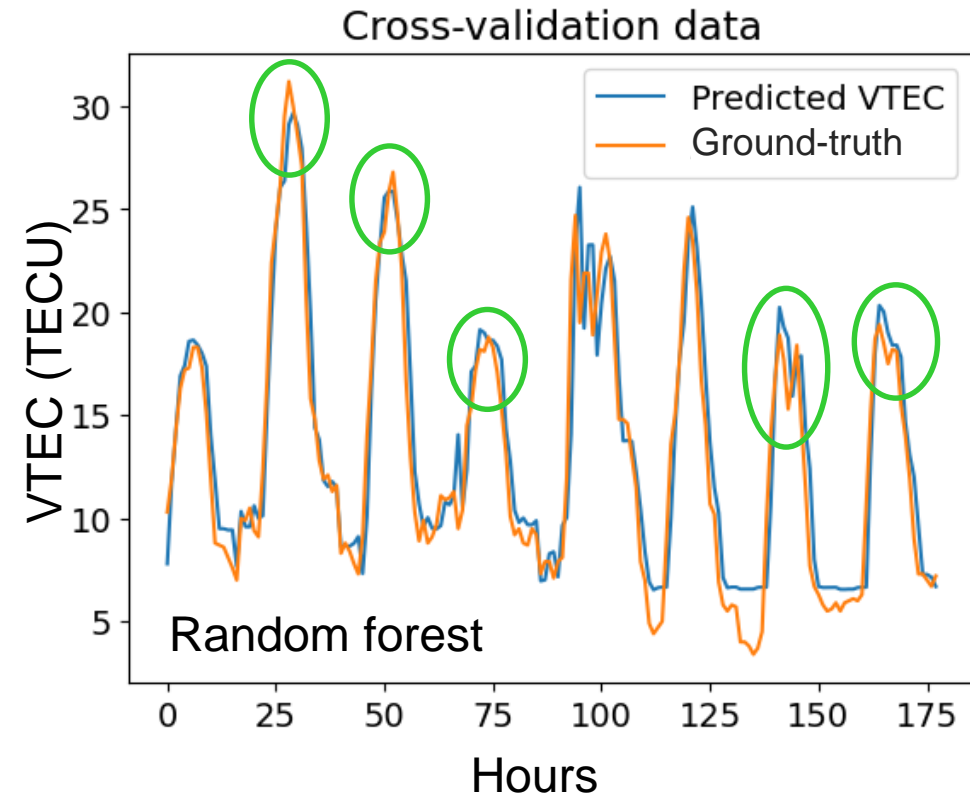
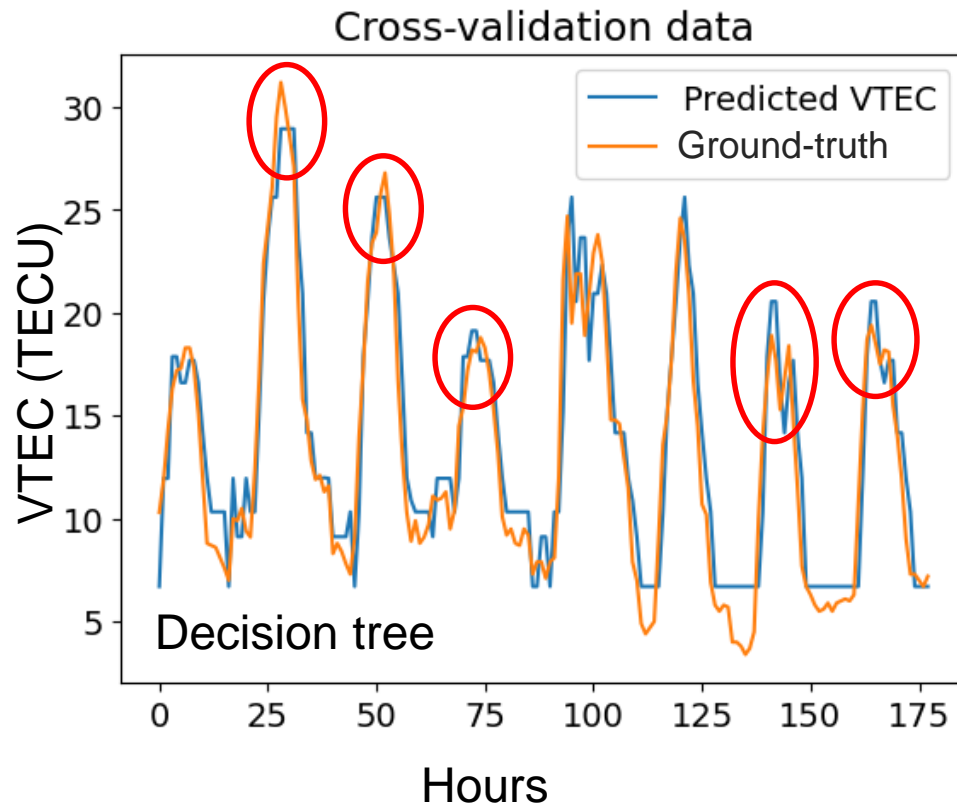
Final outcome: average VTEC in the particular leaf node.

Decision tree

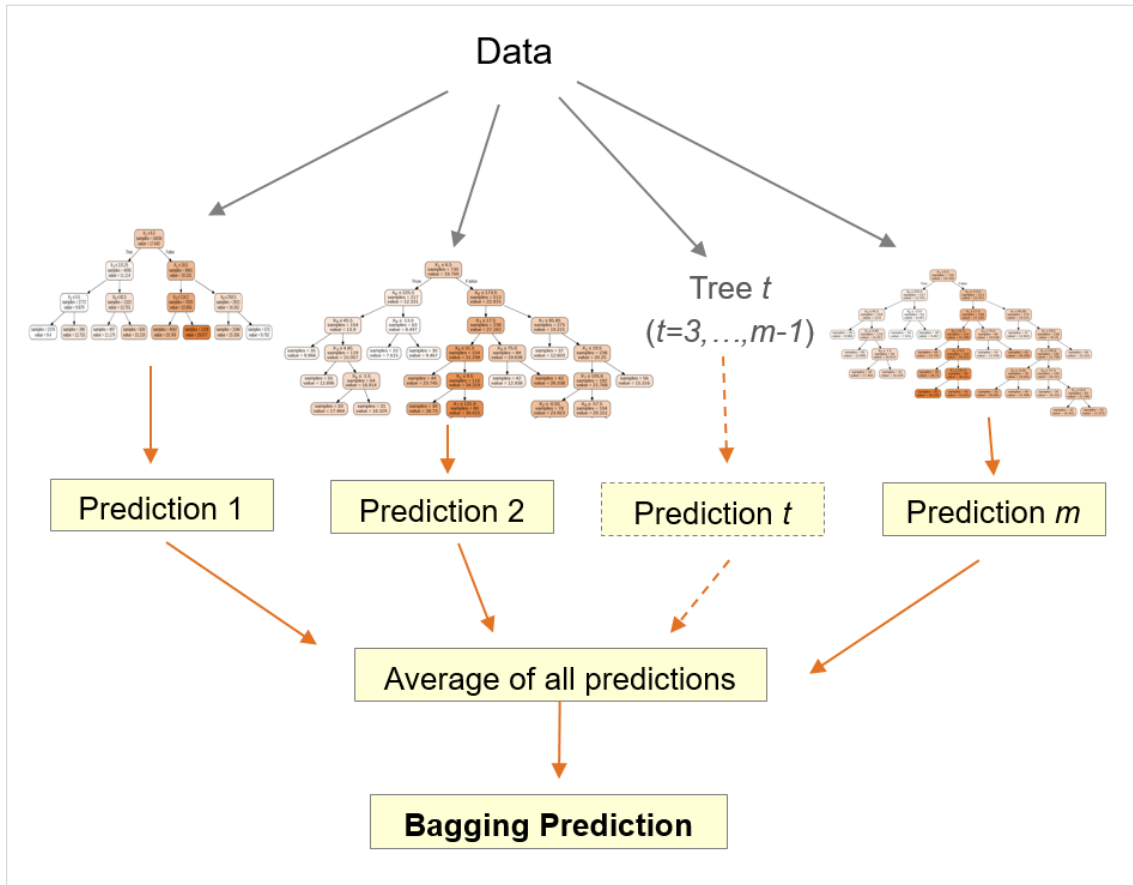
- ✓ Highly interpretable → follows a similar pattern to human thinking
- ✓ Lack of smoothness

Overcome issues → combining many trees

- ✓ Prediction smoother, more robust and more accurate
- ✓ Cost: reducing interpretability by increasing number of trees



Tree-based ensemble

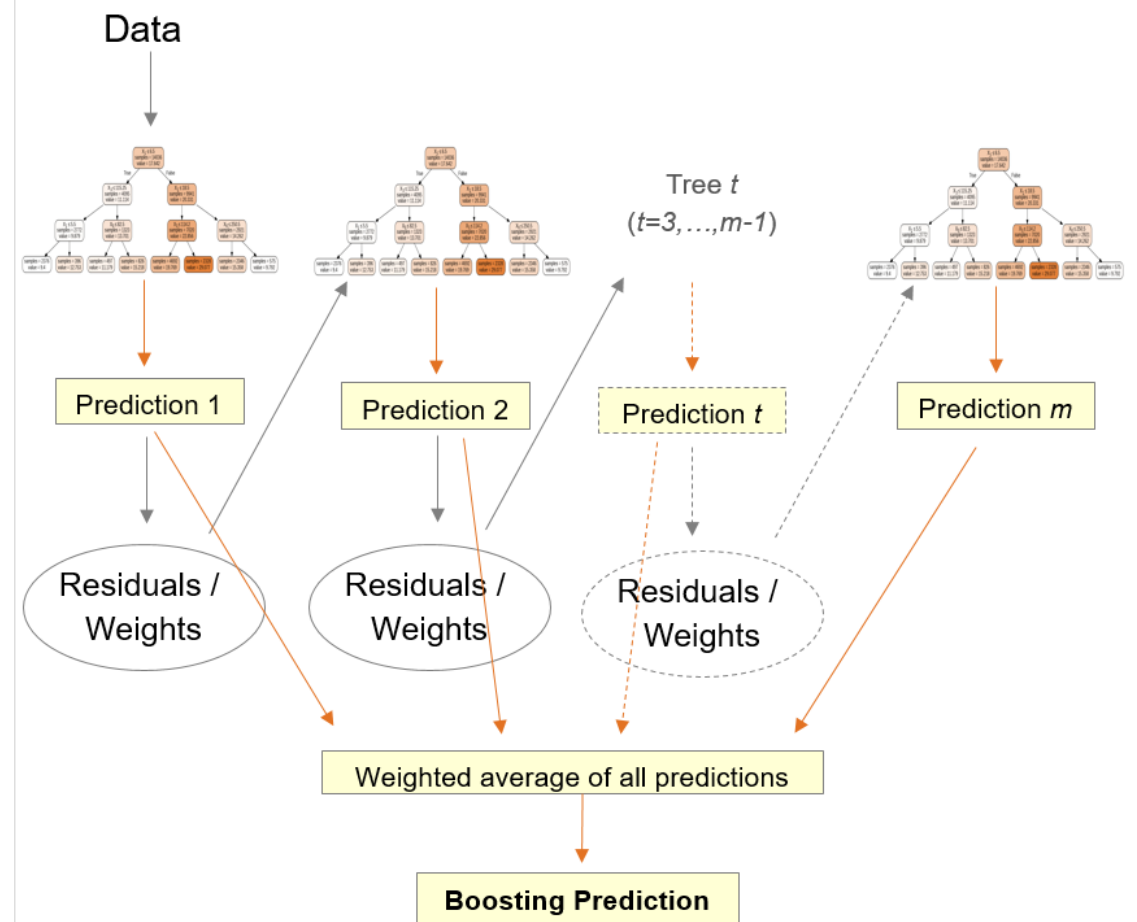


Bagging (Parallel Ensemble Learning):

- Random Forest (multiple randomized trees)

Boosting (Sequential Learning):

- Adaptive Boosting - AdaBoost (weighted obs.)
- Gradient Boosting - GBoost (residuals)



2. Quantifying uncertainties

- ✓ Define the **accuracy and precision** of VTEC prediction,
- ✓ Quantify the level of **trust** in VTEC prediction,
- ✓ Increase the **reliability** of VTEC predictions.

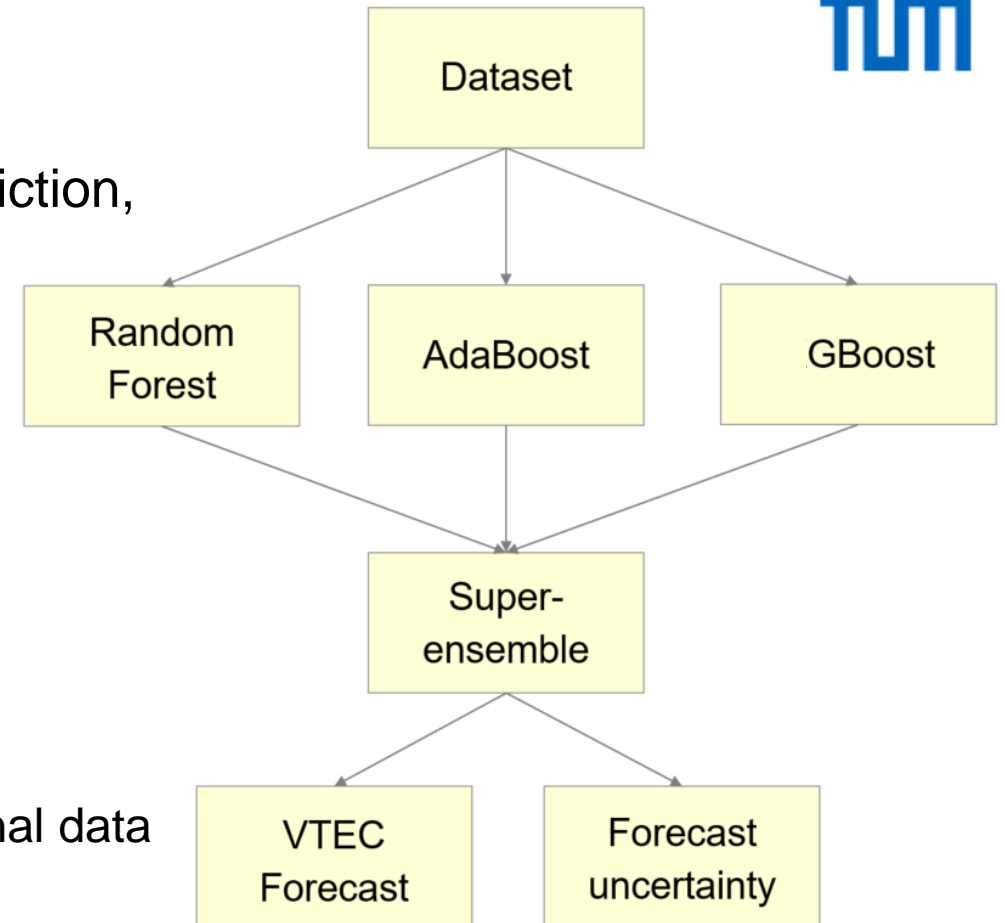
I. Multi-model and multi-data ensemble

- VTEC forecast → ensemble mean
- Forecast uncertainty → ensemble spread (2σ)
- 3 datasets^{*}:
 1. Original data in input and output
 2. Daily differences in input and output
 3. Input: original data + daily differences, output: original data

II. Confidence interval

- Quantile objective loss function
- Applied for GBoost and 3rd dataset
- Quantiles: upper bound $\alpha = 0.95$, lower bound $\alpha = 0.05$

^{*} Observations were preprocessed / cleaned before training.



$$\mathcal{L}(e_i|\alpha) = \begin{cases} \alpha \cdot e_i & \text{if } e_i \geq 0, \\ (\alpha - 1) \cdot e_i & \text{if } e_i < 0 \end{cases}$$

$$e_i = y_i - f(\mathbf{x}_i)$$

$$\mathcal{L}(\mathbf{e}|\alpha) = \frac{1}{N} \sum_{i=1}^N \mathcal{L}(e_i|\alpha)$$

1-day VTEC Forecasting, Data (time sampling 1h)

Input data:

- Time: Hour of day and Day of year (DOY)
- Sunspot number R (daily)
- Solar radio flux F10.7 (daily)
- Solar wind plasma speed (hourly)
- Bz index (hourly)
- AE index (hourly)
- Dst index (hourly)
- Kp index (3-hour)
- VTEC from GIM CODE (hourly)
 - 10E 70N, 10E 40N, 10E 10N
- VTEC moving averages over previous 4 days and 30 days
- Derivatives of VTEC

Time:
t

Output data:

- VTEC (GIM CODE)
 - 10E 70N,
 - 10E 40N,
 - 10E 10N

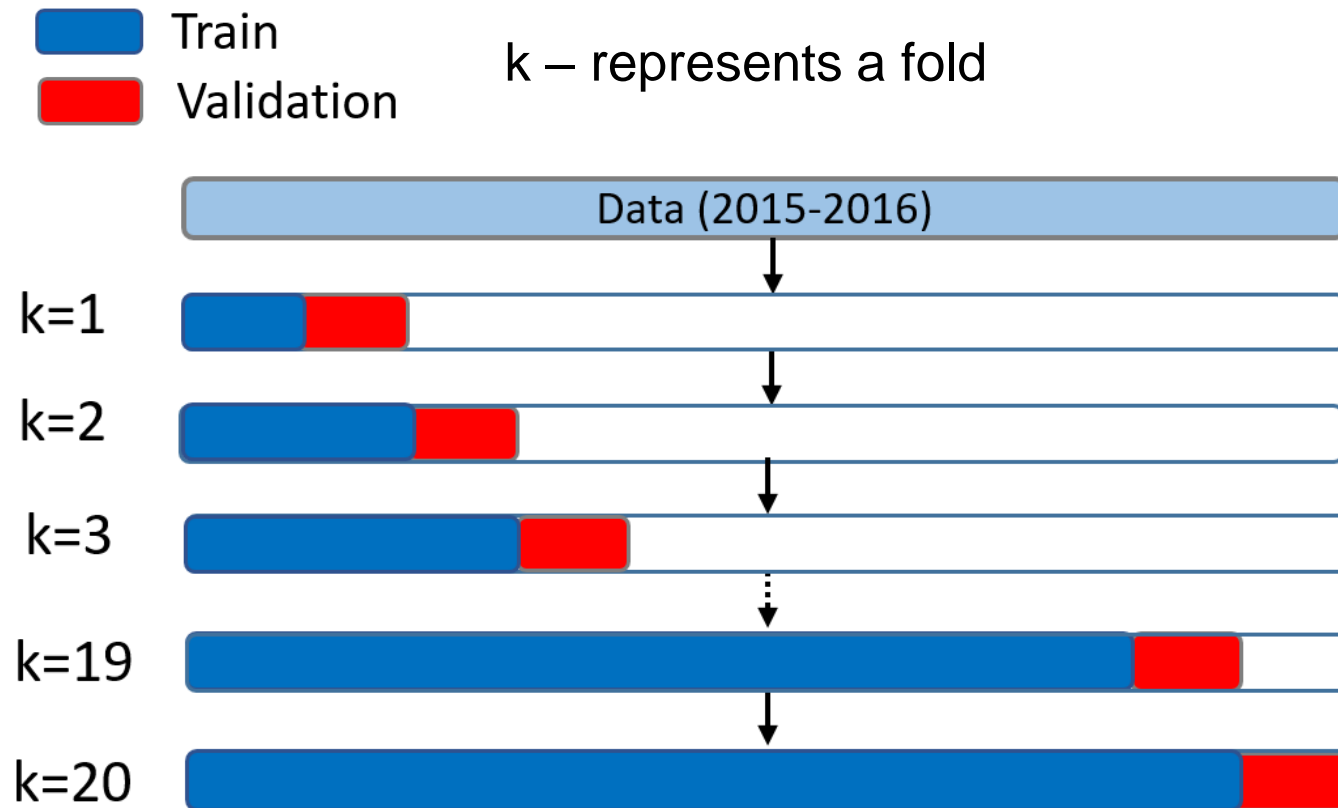
Time:
t+24h

Data split:

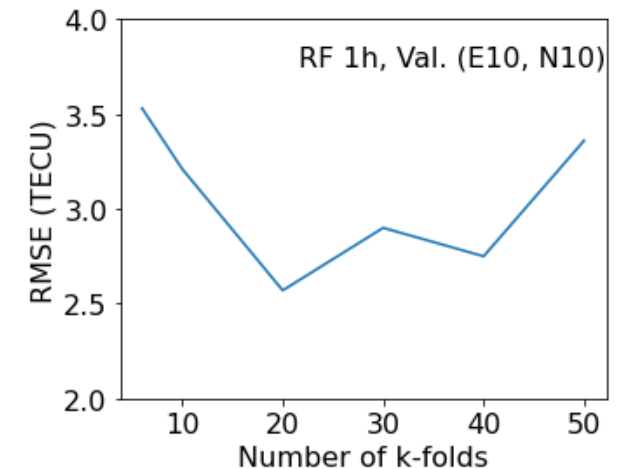
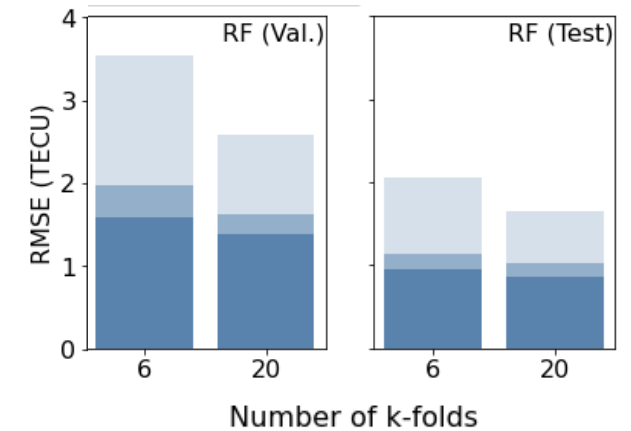
- Training
 - Cross-validation
 - Test
- 2015 - 2016
2017

Model training and optimization / evaluation

- Temporal structure of time series → Cross-validation on a rolling basis
- Evaluate model performance in a robust way

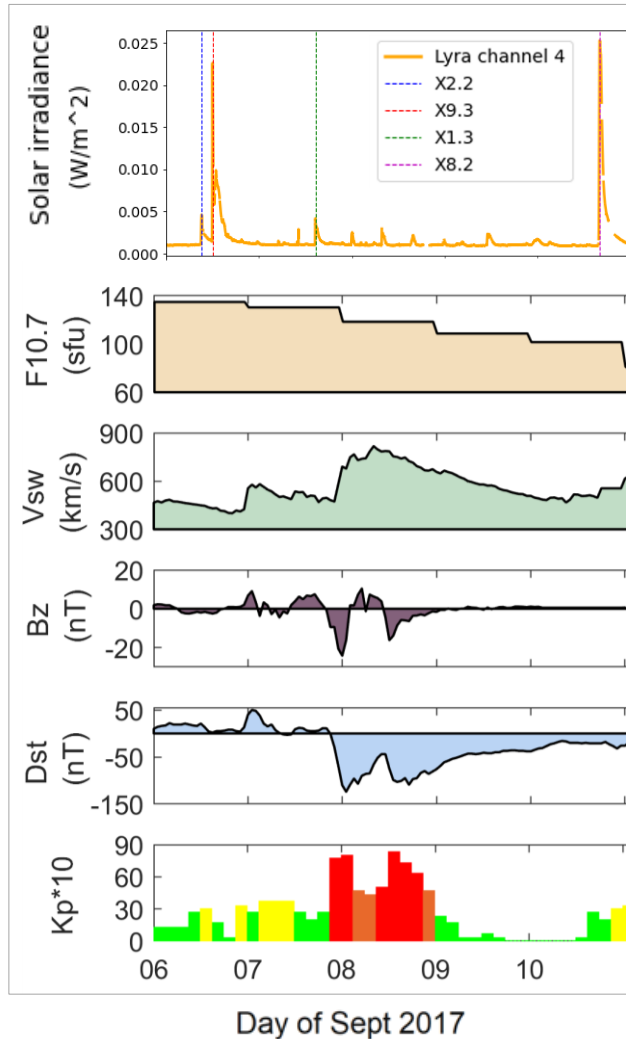


■ 10E 10N ■ 10E 40N ■ 10E 70N

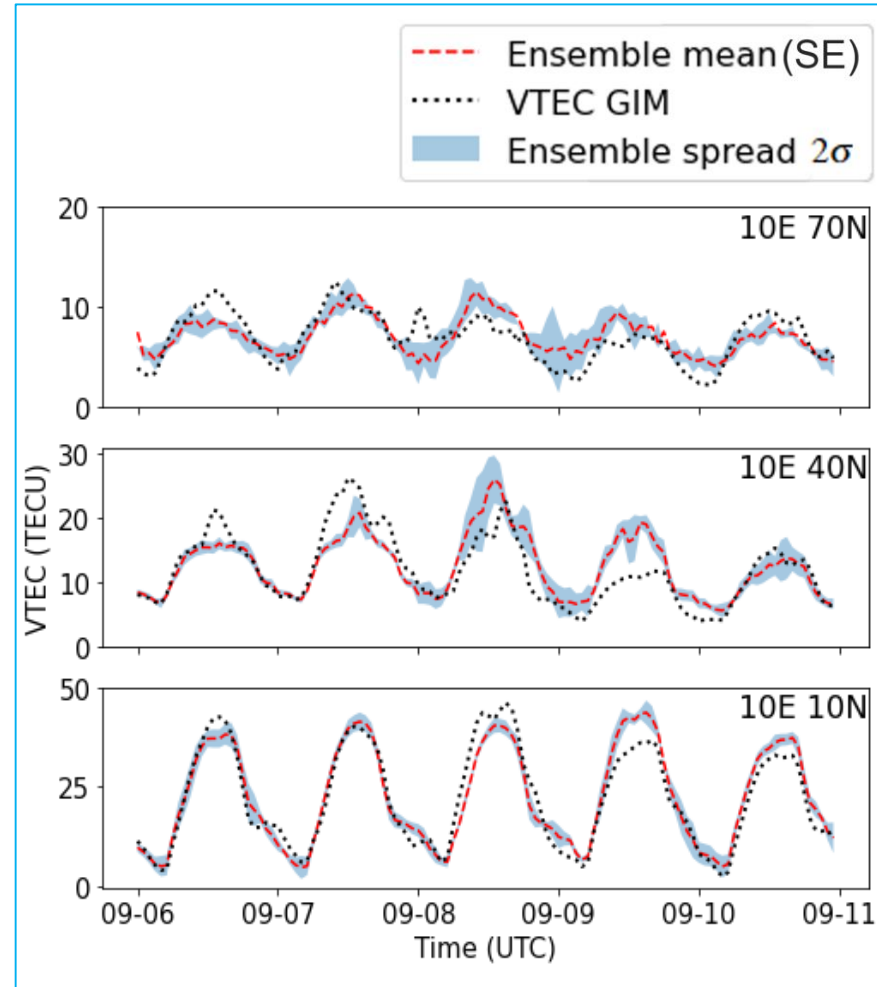


Results: September 2017 space weather events

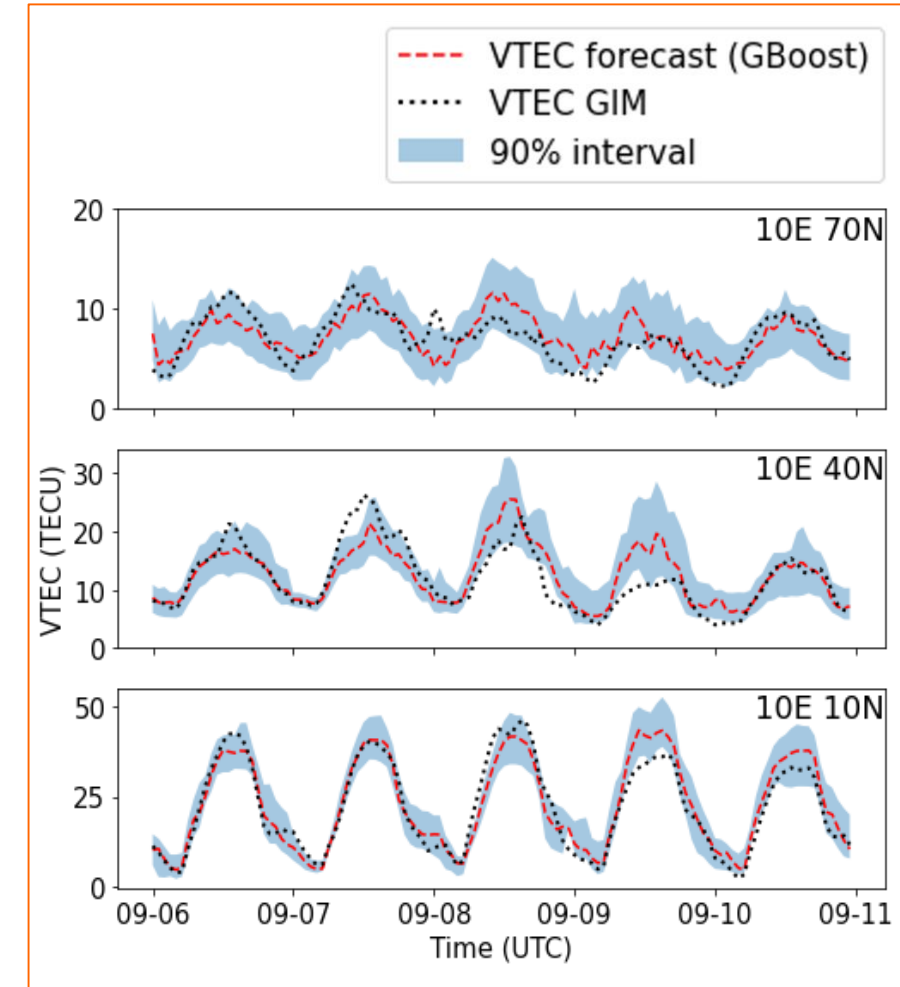
Space weather overview



UQ: Ensemble method

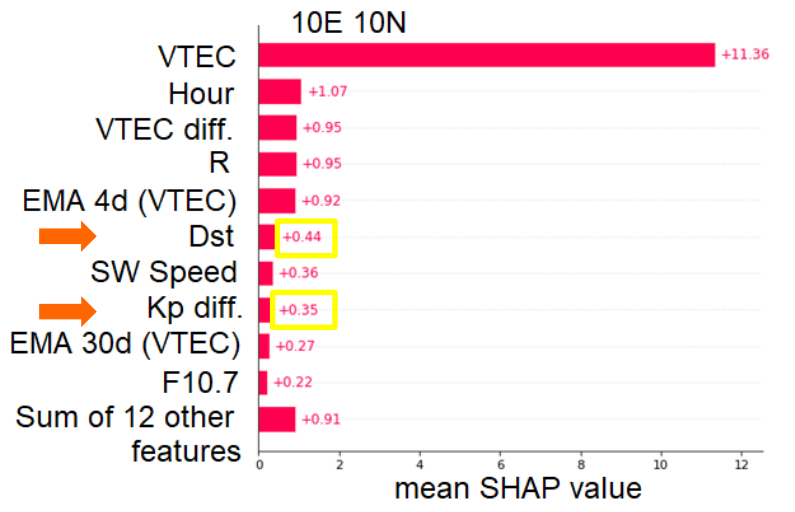
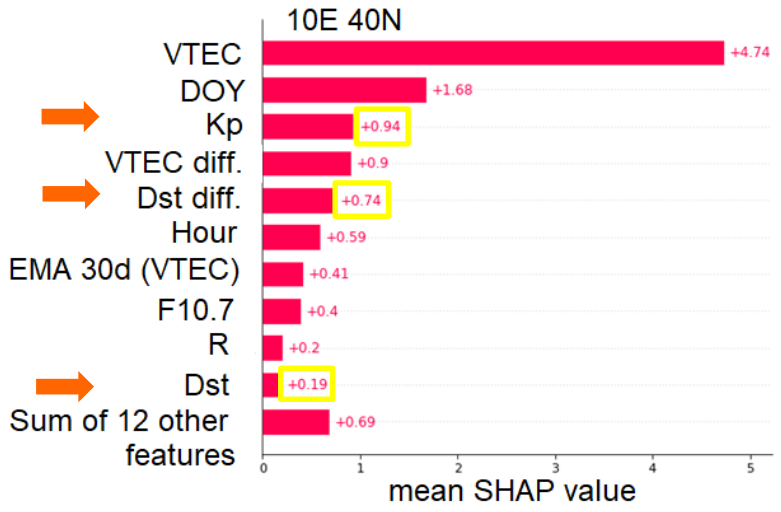
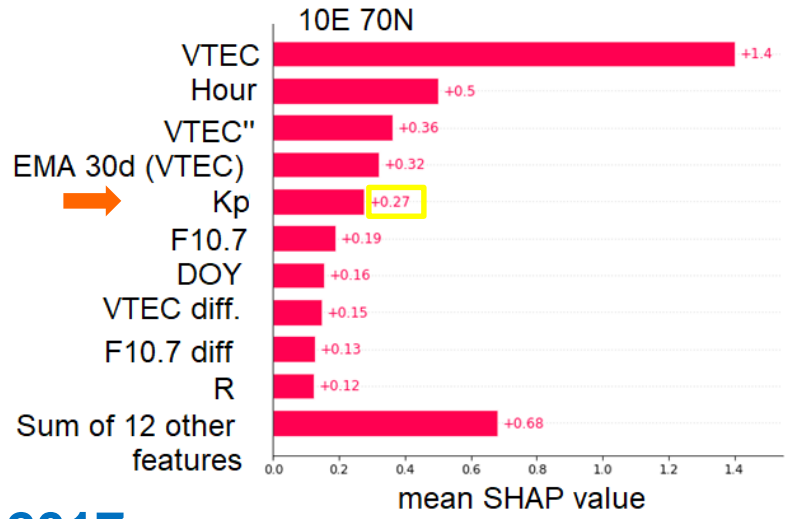


UQ: Confidence intervals

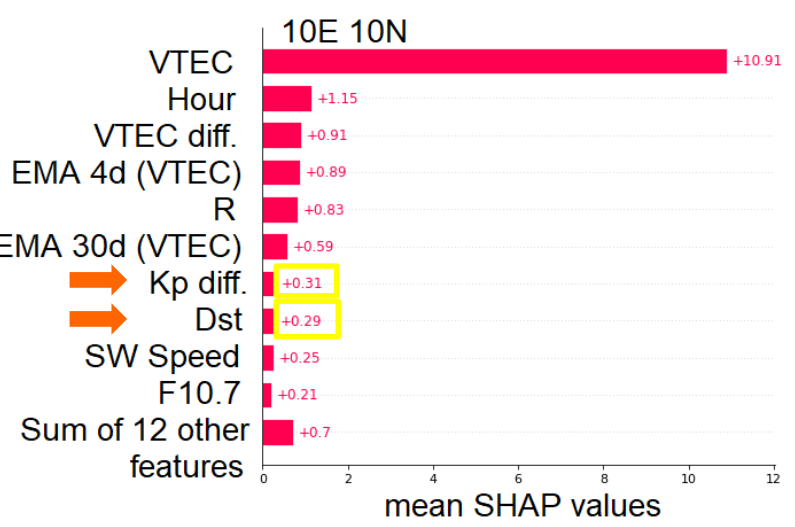
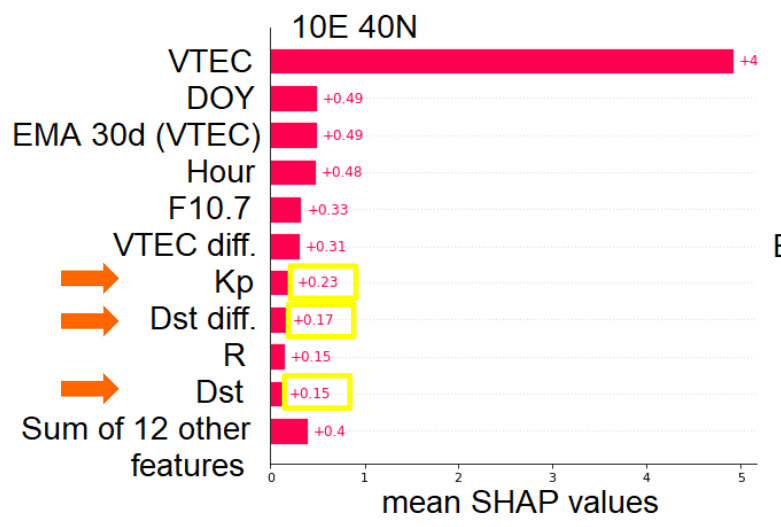
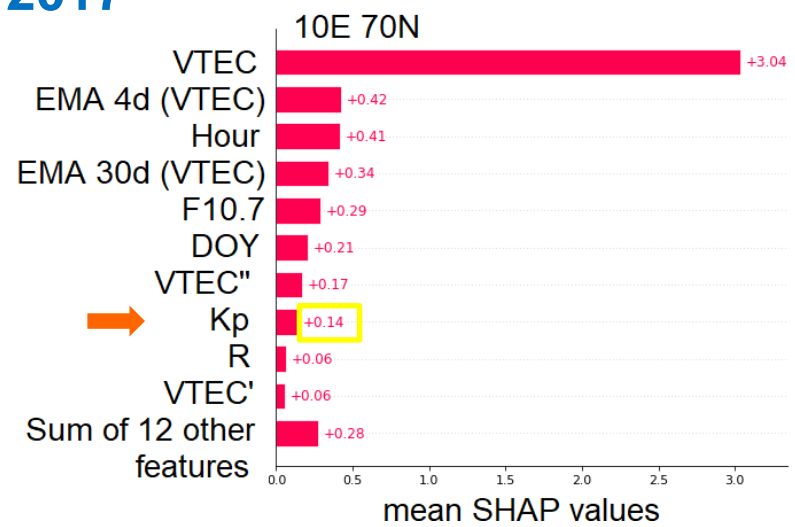


Average features impact on the output

Sept 8-9, 2017

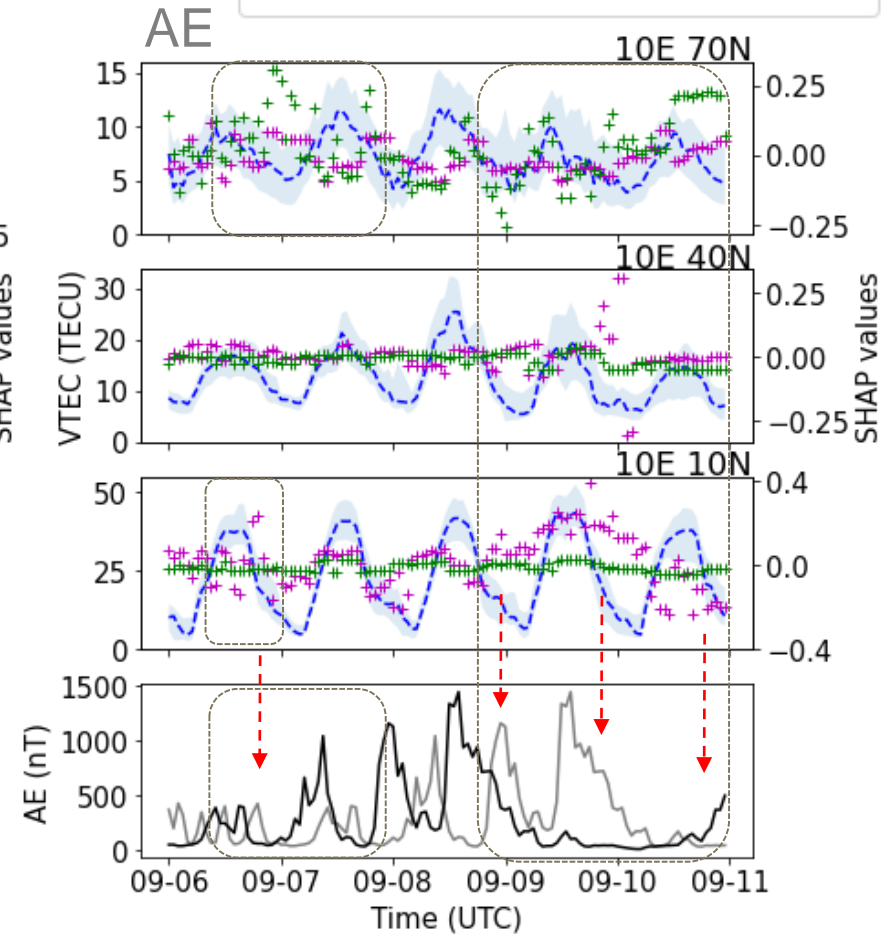
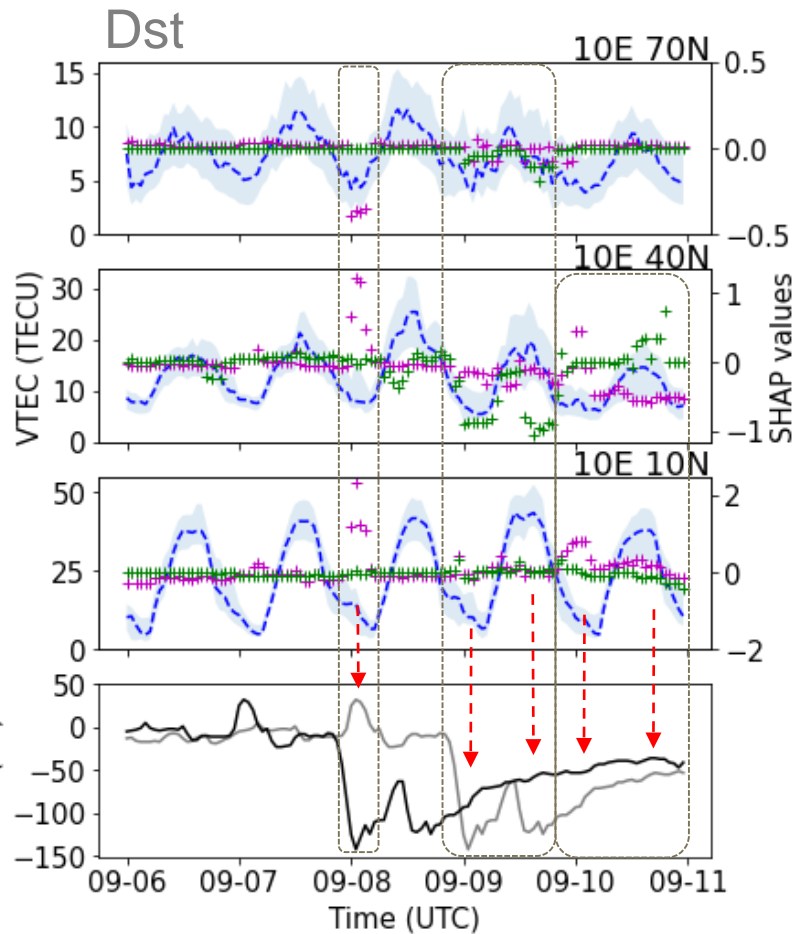
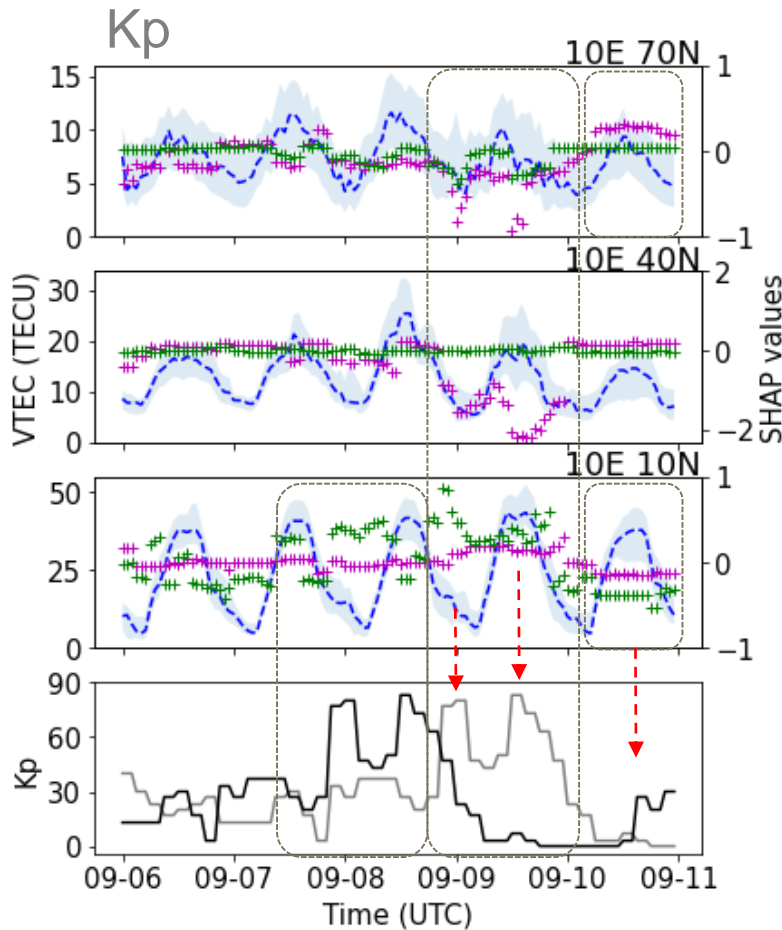
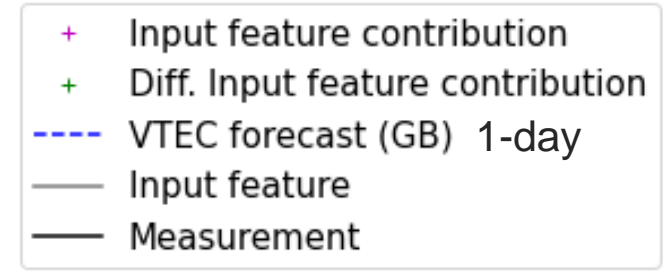


2017



Geomagnetic features → VTEC forecast

Positive SHAP value → increase of VTEC value
 Negative SHAP value → decrease of VTEC value
 0 → no contribution



Conclusion

- Learning algorithms: **interpretability** / **performance** trade-off, amount of data
- The **uncertainty information** defines the **reliability** and **precision** of VTEC predictions
- Uncertainty quantification allows to assess the **trustworthiness of predictions**
- Ground-truth VTEC within predicted confidence intervals for space weather events
- Higher contribution from geomagnetic-related input features during the storm

Thank you for your attention!

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